# Balancing Wheeled Robot 

A dissertation submitted by

Ho, Khoon Chye Randal
in fulfillment of the requirements of

## Courses ENG4111 and 4112 Research Project

towards the degree of

## Bachelor of Engineering (Electrical and Electronics)

Submitted: October, 2005

## Certification

I certify that the ideas, designs and experimental work, results, analyses and conclusions set out in this dissertation are entirely my own effort, except where otherwise indicated and acknowledged.

I further certify that the work is original and has not been previously submitted for assessment in any other course or institution, except where specifically stated.

Ho, Khoon Chye Randal
Student Number: 0050027382

Signature

## Date

## Faculty of Engineering and Surveying

## ENG4111 \& ENG4112 Research Project

## Limitations of Use

The Council of the University of Southern Queensland, its Faculty of Engineering and Surveying, and the staff of the University of Southern Queensland, do not accept any responsibility for the truth, accuracy or completeness of material contained within or associated with this dissertation.

Persons using all or any part of this material do so at their own risk, and not at the risk of the Council of the University of Southern Queensland, its Faculty of Engineering and Surveying or the staff of the University of Southern Queensland.

This dissertation reports an educational exercise and has no purpose or validity beyond this exercise. The sole purpose of the course pair entitled "Research Project" is to contribute to the overall education within the student's chosen degree program. This document, the associated hardware, software, drawings, and other material set out in the associated appendices should not be used for any other purpose: if they are so used, it is entirely at the risk of the user.

## Prof G Baker

Dean
Faculty of Engineering and Surveying

## Acknowledgements

I would like to express sincere thanks to my USQ project supervisor Mr. Mark Phythian local supervisor for their guidance and support throughout the duration of the balancing wheeled robot project. I have learned a lot under their guidance, be it practically or theoretically.

In addition to that, I would also like to thank lab supervisor Mr. Voon who has help me to arrange the suitable lab hours to use during the course of the project. He is indeed a nice person as no matter how busy he would offer some time to give some invaluable advice on certain issues.

Other than that I am also grateful to my friends who have help and guide me in searching for important notes and books.

Finally, I would like to thank my parents for their moral support as I can count on them whenever I am down and upset.


#### Abstract

Inverted pendulum has long been the interest of control engineers. The system is unique in such a way that defies the logic of human brain. Moreover, the system inherited the non-linearity attributes, which is part of every systems on earth.

The concept of two wheeled balancing robot is based on the inverted pendulum theory. A suitable control system is needed to control the system so that it is balanced and stable. The main purpose of this project is to use a good control strategy to keep the body of the robot upright.

This dissertation applies the idea of non-linear control strategy and analyses its effectiveness. The non-linear control strategy requires a good understanding of the inverted pendulum system. The knowledge is then implemented in programming to program the microcontroller. This is particularly important in low-level assembly language, which is used in this project.

Two types of semiconductor sensors to provide tilt information to the robot to balance are applied. The sensors used are gyroscopes and accelerometer. The performance of the sensors is then evaluated based on stability.

In addition to that, it is important to design a reliable motor driver to control the speed and direction of the motors, which is central to the balancing process. The method used is the h -bridge circuit. Since there are two different motors are controlled separately, it is best to control the speed so that the motors work in harmony with each other, thus balancing the robot better.


## Nomenclature

The following are the variables being used in modeling the balancing robot.
x Linear displacement
\& Linear velocity
\& Linear acceleration
$\theta_{\mathrm{rc}} \quad$ Rotation angle of robot chassis
$\boldsymbol{\vartheta}_{r c} \quad$ Angular velocity of the robot chassis
Ac Angular acceleration of robot chassis
$\boldsymbol{\vartheta}_{w h} \quad$ Angular velocity of the wheel
$\overbrace{w h} \quad$ Angular acceleration of the wheel
$\mathrm{C}_{1} \quad$ Applied torque from motor to left wheel
$\mathrm{C}_{\mathrm{r}} \quad$ Applied torque from motor to right wheel
$\mathrm{P}_{1,}, \mathrm{P}_{\mathrm{r}}$ Reaction forces between the wheel and chassis
$\mathrm{H}_{1}, \mathrm{H}_{\mathrm{r}}$
$\mathrm{H}_{\mathrm{fr}}, \mathrm{H}_{\mathrm{lr}}$ Friction forces between the wheels and the ground
$\mathrm{g} \quad$ Gravitational acceleration, $9.81 \mathrm{~m}^{-2}$
$J_{r c}$ Moment of inertia of robot chassis
$J_{w h}$ Moment of inertia of wheelw
$M_{w h}$ Mass of the robot wheels
$M_{r c}$ Mass of robot chassis
$l \quad$ Distance between the centre of the wheels and robot centre of gravity
r Radius of the wheel

## Table of contents

Page
Certification ..... i
Limitation of Use ..... ii
Acknowledgements ..... iii
Abstract ..... iv
Nomenclature ..... v
Chapter 1: Literature review
1.0 Balancing Robots ..... 1
1.1 Control System ..... 2-3
1.2 Data Acquisition ..... 4
1.3 Kalman Filter ..... 4
Chapter 2: Introduction
2.0 Balancing Wheeled Robot Concept ..... 5
2.1 Balancing Process ..... 5-6
2.2 System Modeling
2.2.1 Wheel Modeling ..... 7-9
2.2.2 Chassis Modeling ..... 10-13
2.3 Approach ..... 14

## Chapter 3: Hardware

3.0 Motor Selection ..... 15
3.1 Speed Calculation ..... 15-16
3.2 Motor Capacity
3.2.1 Speed Measurement ..... 17
3.2.2 Results ..... 18
3.4 Robot Chassis Design
3.4.1 Robot Weight ..... 19
3.4.2 Materials ..... 19
3.4.3 Robot Response ..... 19
3.4.4 Gears Selection ..... 20
3.4.5 Motor Mounting ..... 20
3.4.6 Aluminum Rod Fabrication ..... 21
3.4.7 Rigidity ..... 21
3.4.8 Robot Chassis Construction ..... 22
Chapter 4: Sensors
4.1 ADXRS 300 Gyro ..... 23
4.2 Coriolis Acceleration ..... 24
4.3 Coriolis Acceleration on Gyro ..... 24-25
4.4 Measuring Coriolis Acceleration ..... 25-26
4.5 Advantages ..... 26
4.6 Axis Selection ..... 27
4.7 Mounting ..... 28
4.8 ADXRS Gyro as Tilt Meter ..... 29
4.9 Measurement Range ..... 29
4.10 ADXL Accelerometer ..... 30
4.11 Calibration
4.11.1 Power Supply Decoupling ..... 30
4.11.2 Capacitors ..... 31
4.11.3 Calculation ..... 31
4.11.4 Software Approach ..... 32-33
4.12 Overall Balancing Program
4.12.1 Programming Approach ..... 34
Chapter 5: Stability Analysis
5.1 Differential Drive Motor Control (While Standstill) ..... 36
5.2 Sensor Fusion ..... 36-38
5.3 Averaging ..... 39
5.4 Differential Drive Motor Control (While Traveling) ..... 39
Chapter 6: Motor Control
6.1 Pulse Width Modulation ..... 40
6.2 H-bridge design
6.2.1 Introduction ..... 41-43
6.3 Design Consideration ..... 43-44
6.4 Totem-pole Circuit ..... 45-46
6.5 Unwanted Situation ..... 46
6.6 Experiment ..... 47
6.7 Results
6.7.1 Pulse Train ..... 47
6.7.2 Current Surge ..... 48
6.7.3 Noise Isolation ..... 48
Chapter 7: Microcontroller
7.1 Reasons ..... 49-50
7.2 Memory ..... 51
7.3 Time Consideration
7.3.1 Oscillators ..... 52
7.4 Software ..... 53
7.5 Arithmatic Operation ..... 54-55
7.5.1 Trade-off ..... 56
Chapter 8: PCB Design Consideration ..... 57
Chapter 9: Discussion \& Conclusion
9.1 Result
9.1.1 Gyro Mounting ..... 58
9.1.2 Accelerometer ..... 58
9.2 Reasons ..... 58-59
9.3 Incomplete tasks
9.3.1 Gyro-Accelerometer Combo ..... 59
9.4 Conclusion
9.4.1 Recommendation for Future Work ..... 60
References ..... 61-63
Appendix A ..... 64-66

## List of Figures

Page
Figure 1: Difference between linear and non-linear response ..... 3
Figure 2: Inverted and non-inverted pendulum ..... 5
Figure 3: Equilibrium or Balanced State ..... 6
Figure 4: Tilted or Unbalanced State ..... 6
Figure 5: Free body diagram of the wheel ..... 7
Figure 6: Inverted Pendulum Free body diagram ..... 9
Figure 7: Balancing robot control system ..... 13
Figure 8: Speed measurement using tachometer/stroboscope ..... 17
Figure 9: Aluminum Gear mounting ..... 20
Figure 10: Motor Mounting ..... 20
Figure 11: Aluminum rod fabrication and mounting ..... 21
Figure 12: Nut tightening ..... 21
Figure 13: Robot Chassis ..... 22
Figure 14: Cut away view of robot base mounting ..... 22
Figure 15: ADXRS 300 Gyro ..... 23
Figure 16: Coriolis acceleration on earth ..... 24
Figure 17: Gyro rotation behaviour ..... 25

Figure 18: ADXRS inner structure 25
Figure 19: Complete inner gyro structure 26
Figure 20: ADXRS 300 Gyro Axes 27
Figure 21: Gyro mounting 28
Figure 22: Gyro characteristic curve 29
Figure 23: PCB power supply coupling 30
Figure 24: Duty cycle decoding scheme 32

Figure 25: Pulse Width Modulation waveform 40

Figure 26: Motor clockwise turn 41
Figure 27: CEMF current flow 42
Figure 28: Motor counter clockwise turn 43
Figure 29: Totem-pole and P-channel Mosfet 45
Figure 30: N-channel MOSFET motor driver 47
Figure 31: Pulse train waveform 47
Figure 32: Clean pulse train waveform 48
Figure 33: Noise corrupted pulse train waveform 48
Figure 34: Microcontroller schematic diagram 49
Figure 35: Microcontroller memory 51
Figure 36: MPLAB interface program 53

## List of Tables

Page
Table 1: Motor O Speed Characteristics ..... 18
Table 2: Motor X Speed Characteristics ..... 18
Table 3: Analog to digital conversion ..... 34
Table 4: H-bridge circuit components operation ..... 44
Table 5: MOSFET's operation ..... 45
Table 6: Comparison of microcontroller features ..... 49

## Chapter 1: Literature Review

This section provides an insight and literature review to the current technology available to construct a two-wheel self balancing robot. It also highlights various methods used by researches on this topic.

### 1.0 Balancing robots

The concept of balancing robot is based on the inverted pendulum model. This model has been widely used by researches around the world in controlling a system not only in designing wheeled robot but other types of robot as well such as legged robots.

Researches at the Industrial Electronics Laboratory at the Swiss Federal Institute of Technology have built a prototype two wheel robot in which the control is based on a Digital Signal Processor. A linear state space controller using information from a gyroscope and motor encoder sensors is being implemented to make this system stabilise. (Grasser et al.2002).

Another two wheeled robot called 'SEGWAY HT' is available commercially (Dean Kamen ,2001) . It is invented by Dean Kamen who has design more than 150 systems which includes climate control systems and helicopter design. An extra feature this robot has is that it is able to balance while a user is standing on top of and navigate the terrain with it. However, this uses five gyroscopes and a few other tilt sensors to keep it balanced.

Next is the small scale robot, Nbot which is similar to JOE is built by David. P Anderson. (Anderson, David.P ) This robot uses a commercially available inertial sensor and position information from motor encoder to balance the system. This robot has won the NASA cool robot of the week in the year 2003.

Steven Hassenplug used a more innovative approach to construct a balancing robot (Steve Hassenplug, 2002). The chassis of the body is constructed by using the LEGO Mindstorms robotics kit. The balancing method of controlling the system is unique with two Electro-Optical Proximity Detector sensors is used to provide the tilt angle information for the controller. This omits the conventional use of gyroscope that has been used by previous robot researchers.

### 1.1 Control System

Over the years there are only two types of control being used by researchers in controlling a system. The types of control is categorised as linear and non-linear control.

In some instances, the linear control is sufficient to control a system. One of the most widely used is the Proportional Derivative Integral controller or better known as the PID controller (Rick Bickle, 2003). The others are linear quadratic controller (LQR), fuzzy logic controller, pole placement controller etc. It is generally accepted that linear control is more popular than non-linear control.

There are two reasons for this. In all cases, the modeling of a system requires a lot of parameters to be considered and applied. Therefore, the system is complex. However, some of the parameters values needed to model the system are small. That is why most researchers would prefer to model their applications in a linear approximation, which is simpler and in some instances effective.

However, in most cases the linear control theory is not suitable for real life implementation, which mostly exhibit non-linear response. For better performance some non-linear approximation can be applied. (J.J. D'Azzo, pg 11)

Figure below shows how a non-linear response can be approximated to a linear response.


Time
Figure 1: Difference between linear and non-linear response

However, it is better to use the non-linear control theory to control the balancing robot system. This is because the system of the balancing robot, which is based on the inverted pendulum concept, is unique and unbalanced in nature ('Inverted Pendulum', Microrobot NA) . Due to this the response is unpredicted.

### 1.2 Data Acquisition

In a paper 'Attitude Estimation Using Low Cost Accelerometer and gyroscope’ presented by Young Soo Suh, it shows the two different sensors which is the accelerometer and gyroscope that exhibits poor results when use separately to determine the attitude which is referred as the pitch angle or roll angle. The factor that contributes to the deviation of the desired result of the gyroscope is due to the drift term. Since the drift increases with time error in output data will also increase.

One of the disadvantages of using accelerometer individually is that the device is sensitive to vibration since vibration contains lot of acceleration components. One solution that Young suggested is that a low pass filter is required to limit the high frequency.

However, the gyroscope can combine with accelerometer to determine the pitch or roll angle with much better result with the use of Kalman filter.

### 1.3 Kalman Filter

The purpose of this filter is to solve problems of statistical nature (Kalman, 1960). Kalman filter is applied based on several mathematical equations that provides computational solution by using the least squares method. In other words, in simple explanation the process is done by averaging a sequence of values. This filter is powerful as it can estimate the past, present and future states. This filter is actually applied in state space equation. Since the program to be used is in assembly this method is not to be used. The averaging method is used instead.

## Chapter 2: Introduction

### 2.0 Balancing Wheeled Robot Concept

Imagine a 2D diagram of an inverted pendulum on the wheel cart. If say, the pendulum falls to the left, the cart should move to the left to try and keep it upwards. This is the same explanation if the pendulum falls to the other side.


Figure 2: Inverted and non-inverted pendulum

### 2.1 Balancing Process

The word balance means the inverted pendulum is in equilibrium state, which its position is like standing upright 90 degrees. However, the system itself is not balance, which means it keeps falling off, away from the vertical axis. Therefore, a gyro chip is needed to provide the angle position of the inverted pendulum or robot base and input into the microcontroller, which the program in itself is a balancing algorithm. The microcontroller will then provide a type of feedback signal through PWM control to the H-bridge circuit to turn the motor clockwise or anticlockwise, thus balancing the robot. This can be further explained in the flow chart.

The figures below show the various position of the robot could be in.


Figure 3: Equilibrium or Balanced State


Figure 4: Tilted or Unbalanced State

### 2.2 System modeling

One of the very first steps for a control system engineer to able to control a system successfully is to understand the system first. An engineer can understand the system better through modeling the system in a free body diagram. In this balancing wheeled robot the modeling is divided into two parts. The first is the wheel model and the second is the chassis model.

After modeling the parameters are combined accordingly in the form of equation. With that the model can be represented by a set of equations in a state space form and controlled using control system theory.

### 2.2.1 Wheel modeling

## Right wheel



## Left wheel



Figure 5: Free body diagram of the wheel

Using the Newton's law of motion, sum of the forces on the x -direction,
$\Sigma \mathrm{F}_{\mathrm{x}}=\mathrm{Ma}$
$\mathrm{H}_{\mathrm{fr}}-\mathrm{H}_{\mathrm{r}}=\mathrm{M}_{\mathrm{wh}}$.

Summing up the moment around the centre of the wheel,
$\Sigma \mathrm{M}=\mathrm{J} \alpha$
$\mathrm{C}_{\mathrm{r}}-\mathrm{H}_{\mathrm{fr}}{ }^{*} \mathrm{r}=\mathrm{J}_{\mathrm{wh}} \hat{G X}_{\mathrm{wh}}$

Rearranging equation (11),
$\mathrm{H}_{\mathrm{fr}}=\frac{\mathrm{C}_{\mathrm{r}}-\mathrm{J}_{\mathrm{wh}} \mathbf{\theta f f}_{\mathrm{wh}}}{\mathrm{r}}$
For the right wheel substitute equation (11) into (10),
$M_{w h}$ \&
For the left wheel,
$\mathrm{M}_{\mathrm{wh}}<\frac{\mathrm{C}_{1}-\mathrm{J}_{\mathrm{wh}} \mathrm{GC}_{\mathrm{wh}}}{\mathrm{r}}-\mathrm{H}_{\mathrm{l}}$

Because the linear motion is acting on the centre of the wheel, angular motion can be transformed into linear motion by simple transformation.

$$
\begin{align*}
& \bigotimes_{w h} \mathrm{r}=\boldsymbol{\theta}_{w h}=\frac{\hat{C}_{k}}{r}  \tag{18}\\
& \boldsymbol{\theta}_{w h} \mathrm{r}=\& \boldsymbol{\theta}_{w h}=\frac{\&}{r} \tag{19}
\end{align*}
$$

For the right wheel,
$\mathrm{M}_{\mathrm{wh}} \frac{C_{r}}{r}-\frac{J_{w h}}{r^{2}} \mathrm{H}_{\mathrm{r}}$

For the left wheel,
$\mathrm{M}_{\mathrm{wh}}=\frac{C_{l}}{r}-\frac{J_{w h}}{r^{2}} \mathrm{H}_{\mathrm{l}}$
Summing up equation (20) and (21),
$2\left(\mathrm{M}_{\mathrm{wh}}+\frac{J_{w h}}{r^{2}}\right) \frac{C_{r}}{r}+\frac{C_{l}}{r}-\left(\mathrm{H}_{\mathrm{l}}+\mathrm{H}_{\mathrm{r}}\right)$

### 2.2.2 Chassis Modeling



Figure 6: Inverted Pendulum Free body diagram

Sum of forces perpendicular to the chassis or pendulum
$\Sigma \mathrm{F}_{\text {perpendicular }}=\mathrm{M}_{\mathrm{rc}} \mathrm{cos} \theta_{\mathrm{rc}}$
$\left(\mathrm{P}_{\mathrm{l}}+\mathrm{P}_{\mathrm{r}}\right) \sin \theta_{\mathrm{rc}}+\left(\mathrm{H}_{\mathrm{l}}+\mathrm{H}_{\mathrm{r}}\right) \cos \theta_{\mathrm{rc}}-\mathrm{M}_{\mathrm{rc}} l \boldsymbol{\theta}_{r \mathrm{c}}-\mathrm{M}_{\mathrm{rc}} \mathrm{s} \sin \theta_{\mathrm{rc}}=\mathrm{M}_{\mathrm{rc}} \mathrm{c}_{\mathrm{c}} \cos \theta_{\mathrm{rc}}$

Sum of forces in the horizontal direction
$\Sigma \mathrm{F}_{\text {horizontal }}=\mathrm{M}_{\mathrm{rc}}$.
$\left(\mathrm{H}_{\mathrm{l}}+\mathrm{H}_{\mathrm{r}}\right)+\mathrm{M}_{\mathrm{rc}} l \underset{r c}{\&} \sin \theta_{\mathrm{rc}}-\mathrm{M}_{\mathrm{rc}} l \underset{\boldsymbol{\theta}_{r c}}{〔} \cos \theta_{\mathrm{rc}}=\mathrm{M}_{\mathrm{rc}}$
Sum of moments around the centre mass of the pendulum

$$
\begin{equation*}
\sum M=\mathrm{J} \alpha \quad, \text { where } \alpha=\underset{G_{r c}}{〔} \tag{25}
\end{equation*}
$$

$-\left(\mathrm{P}_{\mathrm{l}}+\mathrm{P}_{\mathrm{r}}\right) l \sin \theta_{\mathrm{rc}}-\left(\mathrm{H}_{\mathrm{l}}+\mathrm{H}_{\mathrm{r}}\right) l \cos \theta_{\mathrm{rc}}-\left(\mathrm{C}_{\mathrm{l}}+\mathrm{C}_{\mathrm{r}}\right)=\mathrm{J}_{\mathrm{rc}} \underset{\theta_{r c}}{(\mathbb{C}}$
Rearranging equation 25 ,
$-\left(\mathrm{P}_{1}+\mathrm{P}_{\mathrm{r}}\right) l \sin \theta_{\mathrm{rc}}-\left(\mathrm{H}_{1}+\mathrm{H}_{\mathrm{r}}\right) l \cos \theta_{\mathrm{rc}}=\mathrm{J}_{\mathrm{rc}} \underset{r c}{ }\left(\mathbb{C}_{C}^{c}+\left(\mathrm{C}_{1}+\mathrm{C}_{\mathrm{r}}\right)\right.$

Multiplying equation (23) by - ell,
$\left[-\left(\mathrm{P}_{1}+\mathrm{P}_{\mathrm{r}}\right) \sin \theta_{\mathrm{rc}}-\left(\mathrm{H}_{\mathrm{l}}+\mathrm{H}_{\mathrm{r}}\right) \cos \theta_{\mathrm{rc}}\right] l+\mathrm{M}_{\mathrm{rcg}} l \sin \theta_{\mathrm{rc}}+\mathrm{M}_{\mathrm{rc}} l^{2} \theta_{r c}=-\mathrm{M}_{\mathrm{rc}} l \cos \theta_{\mathrm{rc}}$

Substitute equation (27) into equation (28) to eliminate $\left(\mathrm{P}_{1}+\mathrm{P}_{\mathrm{r}}\right)$ and $\left(\mathrm{H}_{1}+\mathrm{H}_{\mathrm{r}}\right)$ term and rearranging the same terms,
$\mathrm{J}_{\mathrm{rc}}\left(\theta_{r c}+\left(\mathrm{C}_{1}+\mathrm{C}_{\mathrm{r}}\right)+\mathrm{M}_{\mathrm{rc}} g l \sin \theta_{\mathrm{rc}}+\mathrm{M}_{\mathrm{rc}} l^{2} \theta_{r c}=-\mathrm{M}_{\mathrm{rc}} l \mathbb{c o s} \theta_{\mathrm{rc}}\right.$
To eliminate $\left(\mathrm{H}_{1}+\mathrm{H}_{\mathrm{r}}\right)$ term for the second equation, equation (24) is inserted into Equation (22) and rearranging the same terms,
$\left(2 \mathrm{M}_{\mathrm{wh}}+\frac{2 J_{w h}}{r^{2}}+\mathrm{M}_{\mathrm{rc}}\right) \frac{C_{r}}{r}+\frac{C_{l}}{r}+\mathrm{M}_{\mathrm{rc}} l \boldsymbol{\theta}_{r c}^{\&} \sin \theta_{\mathrm{rc}}-\mathrm{M}_{\mathrm{rc}} l \boldsymbol{\theta}_{r c} \cos \theta_{\mathrm{rc}}$

Equation (29) and (30) are non-linear equations, and to get linear equations, some linearising or assumption are taken. Let $\theta_{\mathrm{rc}}=\pi+\delta$, where $\delta$ is the small angle from the vertical upward direction. Therefore, $\cos \theta_{\mathrm{rc}}=-1, \sin \theta_{\mathrm{rc}}=-\delta$ and $\frac{d^{2} \theta_{r c}}{d t^{2}}=0$.

The linearised equation representing the whole system is,

$$
\begin{align*}
& \mathrm{J}_{\mathrm{rc}} \boldsymbol{\delta}_{r c}+\left(\mathrm{C}_{\mathrm{l}}+\mathrm{C}_{\mathrm{r}}\right)-\mathrm{M}_{\mathrm{rc}} \mathrm{~g} l \delta+\mathrm{M}_{\mathrm{rc}} l^{2} \mathcal{\delta C}_{r c}=\mathrm{M}_{\mathrm{rc}} l  \tag{31}\\
& \left(2 \mathrm{M}_{\mathrm{wh}}+\frac{2 J_{w h}}{r^{2}}+\mathrm{M}_{\mathrm{rc}}\right) \frac{C_{r}}{r}+\frac{C_{l}}{r}+\mathrm{M}_{\mathrm{rc}} l \delta \mathcal{\delta}_{r c} \tag{32}
\end{align*}
$$

Rearranging the state space representation,

$$
\begin{equation*}
\delta_{\varepsilon_{r c}}=\frac{M_{r c} g l}{J_{r c}+M_{r c} l^{2}} \delta+\frac{M_{r c} l}{J_{r c}+M_{r c} l^{2}} \frac{\left(C_{1}+C_{r}\right)}{J_{r c}+M_{r c} l^{2}} \tag{33}
\end{equation*}
$$

$\left.M_{r c} l{ }^{2} M_{w h}+M_{r c}+\frac{2 J_{w h}}{r^{2}}\right)^{8} \otimes_{r c}^{\&}+\frac{C_{1}+C_{r}}{r\left(2 M_{w h}+M_{r c}+\frac{2 J_{w h}}{r^{2}}\right)}$

The state space equation is obtained as below after substituting equation (33) into (32) and equation (34) into (31) in the form of:

$$
\frac{d \zeta}{d t}=A \bar{\zeta}+B u
$$


where $\varphi=2 M_{w h}+\frac{2 J_{w h}}{r^{2}}+M_{r c}$
and output of

$$
\mathrm{y}=\mathrm{C} \bar{\zeta}
$$

$$
y=\left[\begin{array}{llll}
1 & 0 & 0 & 0  \tag{36}\\
0 & 0 & 1 & 0
\end{array}\right]\left[\begin{array}{l}
x \\
\delta \\
\delta \\
\delta \delta
\end{array}\right]
$$

The C matrix is oriented this way because the position of the wheel base and the robot chassis are interested.

Applying the feedback equation:

$$
\mathrm{u}=\mathrm{r}-\left[\begin{array}{llll}
e & f & g & h
\end{array}\right]\left[\begin{array}{l}
x 1  \tag{37}\\
x 2 \\
x 3 \\
x 4
\end{array}\right]
$$

Whereby $\mathrm{x} 1, \mathrm{x} 2, \mathrm{x} 3$ and x 4 are the states of the state space equation
The feedback equation is the equation that is about to be inserted into the main system, with coefficients e,f,g, and h are the arbitrary chosen values to be experimented (by trial and error) in order to get the robot to balance properly.

Finally the overall balancing robot control system is shown in the figure below.


Figure 7: Balancing robot control system

The term or variable $u$ represents the driving speed of the motor to lift the robot chassis upright. In order to drive the robot chassis upright the motor need to have the required minimum speed to do the task.

The non-linear state space equation is difficult to derive as there are many variables that has to be taken care of. However, the equations (29) and (30) can be represented with the state space equation

### 2.3 Approach

The balancing robot can be controlled using the state space equation with high level language programming such as C. However, after gaining much understanding of the robot system it is logically possible that the balancing robot can be controlled by using the assembly language programming, even though it is quite simplistic as compared to the state space equation previously derived in the modeling section.

The following strategy is applied in the control of balancing robot.

## a) Data acquisition time

The time the microcontroller takes to collect and execute the data obtained. Theoretically if the microcontroller can acquire data and applying control strategy faster than the response of the robot chassis tilts the robot will appear to be balanced and more stable.

## b) The non-linearity control

Applying a control strategy limits the overshoot. For instance, there is no accurate prediction that the motor would not output more speed when in fact the speed required to control (programmed) is lesser. That is why to be on the safe side a few lines of control to limit that possible non-linearity behavior.
c) Proportional band control

This is based on the requirement of the robot from the motor to appropriately control the tilt of the robot. For instance, when the robot tilts further the more speed is required to lift the chassis and vice versa.

## Chapter 3: Hardware

### 3.0 Motor Selection

There are basically two types of motor that are in consideration initially. There are a few reasons why the car wiper motor, which is one of the permanent magnet DC motor, is chosen over stepper motor.

The first is that the stepper motor does not turn on the shaft fast enough. That is the speed of response is slow. This could be detrimental to the balancing robot as the speed that the robot tilts is quite fast and need a motor that could match or have faster response than the robot chassis to lift the chassis to the upright position.

Secondly, the rating speed (in r.p.m) of the stepper motor is not as high as the permanent magnet DC motor. This aspect is also essential in the balancing robot project as heavier robot needs more motor speed from the motor to lift the chassis balanced state.

### 3.1 Speed Calculation

This section focuses on the how to calculate the required speed of the motor to lift the chassis of the balancing robot upright. The rated speed of the motor has to be sufficiently high in order to balance the weight of the robot. If the weight of the robot is more than the motor can handle the robot will not be able to standstill.

Acceleration needed $=5 \mathrm{~ms}^{-2}$
Weight of the wheels and motors $=2 \mathrm{~kg}$

Force to accelerate the 2 kg is $\mathrm{F}=\mathrm{ma}, \mathrm{F}=2 * 5 \mathrm{~ms}^{-1}$

$$
=10 \mathrm{~N}(5 \mathrm{~N} \text { per wheel })
$$

Wheel radius $=0.045 \mathrm{~m}$

Power required from motor would be $\mathrm{P}=\mathrm{v}$ * F

$$
\begin{aligned}
& =2 * 10 \\
& =20 \mathrm{~W}, \text { that is two } 20 \mathrm{~W} \text { motors }
\end{aligned}
$$

Assuming the motors will on average operate at $1 / 2$ their rated voltage, this leads to a factor of 4 reductions in the power output of the motor (from its rated power).

$$
\begin{aligned}
\mathrm{P} & =\mathrm{V}^{2} / \mathrm{R} \\
& =(1 / 2 \mathrm{~V})^{2} / \mathrm{R} \\
& =1 / 4 \mathrm{~V}^{2} / \mathrm{R}
\end{aligned}
$$

So that is 20 W (needed) $* 4=80 \mathrm{~W}$ motors.
Given some tolerance of $5 \%$ of the required power of the motor; therefore a motor power rating of about 84 W is required.

Due to the fact that the angular rate of turn is quite high and in order to make it controllable, the speed should be geared down by a ratio of three 3 (1:3). The speed must not be geared down significantly as it will increase the moment of inertia in the drive mechanism and slows its responsiveness (John Billingsley, 2005).

### 3.2 Motor capacity

After finalising the required speed of a motor needed the next step would be confirming the motor capacity of a motor practically. The information can be obtained by reading the angular rate or speed and power from the motor's datasheet. Since the car wiper motors that obtained is from the spare parts shop another method is needed to get the information. This can be by using a stroboscope/tachometer to measure the angular rate.

### 3.2.1 Speed measurement



Figure 8: Speed measurement using tachometer/stroboscope

The tachometer is positioned as above and a reflector paper is attached to the motor shaft. As the motor shaft turns the tachometer light output is emitted onto the reflector paper, when then reflect the light back to the tachometer to provide a reading. The reading is the angular rate which is in unit r.p.m.

### 3.2.2 Results

Determining the characteristics of the wiper motor:
Motor O (Side wire)

| Voltage, V | Current, A | Angular speed, rpm |
| :--- | :--- | :--- |
| 12 V | 1.3 A | 3100 rpm |
| 10 V | 1.26 A | 2500 rpm |
| 8 V | 1.05 A | 1900 rpm |

Motor O (Centre wire)

| Voltage, V | Current, A | Angular speed, rpm |
| :--- | :--- | :--- |
| 12 V | 0.7 A | 2100 rpm |
| 10 V | 0.68 A | 1780 rpm |
| 8 V | 0.6 A | 1360 rpm |

Table 1 : Motor O speed characteristics

Motor X (Side wire)

| Voltage, V | Current, A | Angular speed, rpm |
| :--- | :--- | :--- |
| 12 V | 1.8 A | 3000 rpm |
| 10 V | 1.7 A | 2300 rpm |
| 8 V | 1.6 A | 1770 rpm |

Motor X (Center wire)

| Voltage, V | Current, A | Angular speed, rpm |
| :--- | :--- | :--- |
| 12 V | 1.22 A | 2085 rpm |
| 10 V | 1.2 A | 1700 rpm |
| 8 V | 1.12 A | 1300 rpm |

Table 2 : Motor X speed characteristics
The speed is measured by using stroboscope/ tachometer and as noted from the experiment, the side wire connection makes the motor turn faster. For general information, wiper motor is a two speed motor whereby user can select whether the faster or the slower speed.

### 3.4 Robot Chassis Design

### 3.4.1 Robot Weight

It is important to consider the overall weight of the robot that one is about to build. This would seriously affect the wheel base design of the robot. The base and the wheel might bend outwards if the overall weight of components is too high for the wheel base to handle.

The drop down list of the total weight contributed:

|  | Quantity | $\mathrm{kg} / \mathrm{quantity}$ | Total weight (kg) |  |
| :--- | :---: | :---: | :---: | :---: |
| Sealed lead acid battery | 2 | 1 | 2 |  |
| Aluminum | - | 0.5 | 0.5 |  |
| Wiper motors | 2 | 0.5 | 2 |  |
| Printed Circuit Boards | 4 | 0.02 | 0.08 | Total $=4.58 \mathrm{~kg}$ |

From the total weight anticipated the robot requires a strong wheel base.

### 3.4.2 Materials

Since the aluminum is strong, light and affordable it is preferably chosen as the material to build the robot base and chassis.

### 3.4.3 Robot Response

The robot falls faster when the robot is shorter. Therefore, a simple experiment can be done by first holding the robot up straight, release and measure the time on how much time it needed to tilt. The taller robot will be easier to control as the responds is slower.

### 3.4.4 Gears Selection

The tooth gear pulley is chosen ahead of the sprocket type. This is because the tooth gear pulley is more durable and the quietest choice. The tooth belt pulley consists of two aluminum gears and a suitable length of belt. This method is easy to use and do not require special skill to mount on the robot.


Figure 9: Aluminum Gear mounting

### 3.4.5 Motor Mounting

Since the wiper motor is quite heavy and a tooth gear pulley is required, it is best that the motor is mounted on top of the robot wheel base. In addition to that ball bearing is embedded into the aluminum side plate in an axis parallel to the motor shaft. This is to reduce the amount of friction imposed on the shaft and this enable the shaft to turn smoothly.


Figure 10: Motor Mounting

### 3.4.6 Aluminum rod fabrication

This step is taken to ensure the portability of the robot. The top and middle rods can be disconnected anytime the user wants.


Figure 11: Aluminum rod fabrication and mounting

### 3.4.7 Rigidity

This type of tightening is to ensure that the robot do not wobble while balancing.


Figure 12: Nut tightening

### 3.4.8 Robot Chassis construction

The chassis of the robot will be constructed of the following designs:


The mounting of the motor to the wheel
Figure 13: Robot Chassis


Figure 14: Cut away view of robot base mounting

## Chapter 4: Sensors

The feedback block of the balancing robot control system consists of sensors that provide information for the robot to move accordingly. There are two types of sensor used in this project, which are the gyro and the accelerometer.

### 4.1 ADXRS 300 Gyro

A person might be curious on how the ADXRS gyro measure data to provide important information to the balancing wheeled robot. It is a general statement that gyro measures angular rate of turn data. ADXRS gyro obtains this data by measuring the coriolis acceleration.


Figure 15: ADXRS 300 Gyro

### 4.2 Coriolis acceleration

Imagine a person standing on a rotating platform near to the center trying to maintain his position to the ground by walking against the rotation at a given speed. Whereas if a person were to maintain his position at the outer rotating platform (away from the center) he has to increase his movement speed. The increase in speed is termed coriollis acceleration (John Green et al, March 2003).


Figure 16: Coriolis acceleration on earth (Source: John Green et al, March 2003)

### 4.3 Coriolis acceleration on gyro

The ADXRS gyro applies the similar effect of the above coriolis acceleration concept. Except that the human is replaced by a small block of mass and forming a damping system. The damping system is designed such that it oscillates in one direction when the platform is rotating. When the damping system moves to the outer surface, it experiences a force to the left (John Green et al, March 2003)


Figure 17: Gyro rotation behaviour
(Source: John Green et al, March 2003)

### 4.4 Measuring coriolis acceleration

The figure below shows the cut off structure of the ADXRS 300 gyro. The structure frame containing the mass is tethered to the substrate perpendicular to the resonating motion (John Green et al, March 2003). The ADXRS primarily utilises the coriolis sense fingers to 'read' the amount of force applied by the mass to it, which in turn 'translates' the force into the voltage reading.


Inner Frame
Resonating Mass
Mass Drive Direction
Springs
Coriolis Sense Fingers

Figure 18: ADXRS inner structure
(Source: John Green et al, March 2003)

Figure below is the complete structure of the ADXRS gyro placed on the moving plate.


Figure 19: Complete inner gyro structure
(Source: John Green et al, March 2003)

### 4.5 Advantages

There are quite a number of reasons why this gyro sensor is chosen over the other sensors such as tilt meters and gyro for helicopters. The reasons are as follows:

## i) Small in size

There is no need to worry about space. Since the gyro is so small that is only about the size of a coin the user can place the gyro on a small empty space on the robot.
ii) Samples available for free (from www.analogdevices.com)

This is great for any researchers that are keen on researching but short of funding.
Analog devices provide this golden opportunity for anyone to try hands-on.

## iii) Has internal conditioning on-chip

This special feature improves the data Most of the information is available on the data sheet as attached on the appendix C.

## iv) Readily available for interfacing with microcontroller chip

There is no need to include extra circuits to interface the ADXRS 300 gyro with microcontroller chip as the signals are compatible with each other.

### 4.6 Axis selection

There are a few axes that can be used. There are named Yaw Axis, Roll Axis and Pitch Axis as shown in figure (A) below. In the balancing robot application only one axis is used. This can be the roll axis in figure (B).


Figure 20: ADXRS 300 Gyro Axes
(Source: John Green et al, March 2003)

### 4.7 Mounting

Due to the fact that measurement of coriolis acceleration is most sensitive when mounted parallel to the ground surfaced the gyro has to be mounted on like the one in the figure (B) above onto the robot. The mounting can be as shown below:


Figure 21: Gyro mounting

### 4.8 ADXRS Gyro as tilt meter

Based on the graph given below the range of values from 2.5 to 4.75 volts can be assigned for clockwise direction tilt and from 2.5 to 0.25 volts the values can be allocated for anti-clockwise direction. For instance, when the microcontroller receive an input on 4.0 volts the chassis will tilt clockwise direction and motor will turn anticlockwise to lift the chassis back up and vice versa.


Figure 22: Gyro characteristic curve

### 4.9 Measurement Range

The ideal measurement range of the graph above does not apply to the practical measurement range. Initially, the measurement range of the gyro is only within 2.3 to 3 volts. Therefore, the method of extending the range is by adding a resistor between the pins CMID and SUMJ of the gyro. This can be found in the data sheet as attached in appendix C4. As found out the measurement range is only from 1.8 volts to 4.9 volts. As a result some adjustment has to be made to enable the microcontroller to measure the voltage values.

### 4.10 ADXL Accelerometer

The purpose of this accelerometer is to be examined whether it can be used as an alternative to find the tilt angle. The second purpose of accelerometer can be considered to use with the gyro chip to stabilize the angular reading drift. This is because it may have an important property, which is the duty cycle to hold the data for a specified period of time before the next sampling edge to calculate and replace the old value.

### 4.11 Calibration

With reference to the data sheet attached at the appendix C3.There are a few electronic components values that needed to be determined before mounting on the printed circuit board designed as attached at the appendix B1.

The primary function of the Rset resistor is to set the PWM period of the accelerometer output, T2. The equation is given in the equation below:
$\mathrm{T} 2=$ Rset $/ 125 \mathrm{MOhm}$

### 4.11.1 Power supply decoupling



Figure 23: PCB power supply coupling

### 4.11.2 Capacitors

The capacitors $C x$ and $C y$ act as the filtering system to reduce the external noise that might affect the overall performance of the accelerometer.

Choosing the low pass filter bandwidth to be 100 Hz
Using the equation: $\mathrm{F}_{-3 \mathrm{~dB}}=1 /(2 \pi(32 \mathrm{KOhm}) * \mathrm{C}(\mathrm{x}, \mathrm{y}))$
Therefore, the capacitance value would be $=0.05 \mathrm{uF}$

### 4.11.3 Calculation

The calibration of ADXL 213 is done by utilizing the earth's gravity as a reference input. The X and Y axes are properly aligned horizontal to the earth such that both axes experience 0 g . A microcontroller is told to read the duty cycle output T1 and period T2 from each of the axes.

The accuracy can be improved by average the readings of T1 and T2. These values are used as the fixed values to be used in calculating the acceleration after calibration mode.

Zcal $=(\mathrm{T} 1 \mathrm{max}-\mathrm{T} 1 \mathrm{~min}) / 2$
The bit scale factor is to be found next. This is to determine the resolution (in bits) of the acceleration calculation as shown below:
$\mathrm{K}=(\mathrm{T} 2 *$ bit scale factor $) /(\mathrm{T} 1$ max- T 1 min$)$

### 4.11.4 Software Approach

T2actual is the measurement of T 2 . This formula offsets the 0 g value for changes in T 2 due to drift. The steps below are actually the method that is used to sample the edges of the output pulse of the accelerometer output.


Figure 24: Duty cycle decoding scheme

The flow chart below illustrates the sampling of the output edges


As can be seen above only the output pulse at X pin is being sampled. This is because one axis is sufficient in this application. After sampling the time values the Acceleration and tilt value of axis can be found by using the formula below:

Acceleration $=\mathrm{K} *(\mathrm{~T} 1-$ Zactual $) /$ T2actual
Zactual $=($ Zcal * T2actual)/T2cal
Full program listing is attached at appendix D

### 4.12 Overall Balancing Program

### 4.12.1 Programming Approach

The ADXRS 300 Gyro output is in the form of analog values. Therefore, the Analog to Digital Converter (ADC) Module of the microcontroller is being utilised.

Since the resultant registers storage is of 10 bits wide and the maximum voltage used is 5 V therefore the assigned analog voltage to digital form is as shown in table 3 .

One bit value is : $\left(2^{\wedge} 10\right) / 5=1023 / 5=204.6$ or equal to 205

| Analog (v) | Multiplier | Digital |
| :---: | :---: | :---: |
| 1 | 205 | 205 |
| 1.5 | 205 | 308 |
| 2 | 205 | 410 |
| 2.5 | 205 | 513 |
| 3 | 205 | 615 |

Table 3: Analog to digital conversion
The resultant value is being stored in ADRESH and ADRESL registers.
After that the computer program will calculate the reading error from the reference, which is 3 V . Then the direction to control will be determined. The program will appropriately choose the correct subroutine, based on error reading calculated to send the appropriate amount of PWM signal to control the motor. In the way it is programmed there are quite a number of PWM subroutines to choose from. This might sound to be a crude technique. There are two reasons for this. Firstly, it has got to do with the design of the h -bridge, which makes the programming even more complex. That is why the internal PWM function of the PIC microcontroller not used. Otherwise the programming could be done better. The second reason would be the robot chassis does not tilt much, therefore does not need much reading for control.

## Chapter 5: Stability Analysis

There are some points need to be taken into consideration. There are a few things that could be done in order to properly balance the robot.

### 5.1 Differential Drive Motor Control (While Standstill)

The method being used here is to manually calibrate the speed of the two differential drive motors such that the shaft not only turns in one direction but with the same speed as well.
The calibration of the two wiper motors are done prior to mount the gyro and accelerometer onto the robot chassis. This is one important step before balancing the robot.

The robot will be quite impossible to balance and might wobble around.

### 5.2 Sensor Fusion

Both the gyro and accelerometer can be used to measure tilt data. However, only the gyro is used to measure the tilt while the accelerometer can be used as a 'stabiliser' to provide stability. There are three important properties that can be utilised from the accelerometer.

First and foremost, the response of the accelerometer sensor is quite slow as compared to the gyro, which only outputs a signal every two cycles (Appendix C, pg ). The other reason is that the output of the accelerometer is in pulse width digital form it could be stated that the output of the accelerometer is more stable than the gyro analog output.

The accelerometer provides a true measure of tilt. For example, the accelerometer will output a digital pulse when the device is in steady state condition. Similarly, accelerometer will change its output accordingly when the device rotates. In other words, the accelerometer will only change its output when the device changes direction.

Unlike the accelerometer the gyro is sensitive to drift, which the value of the output changes with respect to time. For instance, when the gyro rotate to a position, the gyro will give a reading, however, the reading will quickly return to steady state value as there is no angular turn.

Therefore, the accelerometer can be combined with the gyro to offset the drift. The strategy is to utilise the delay in accelerometer to 'hold' the gyro data and only output a signal to the motor driver when the accelerometer 'permits' it. The general process can be better understood through the flowchart


### 5.3 Averaging

Since the gyro outputs data at a high rate the sensor data is quite unstable. In other words, the reading is not linear and it oscillates. That is why the reading needs to be averaged.

This is one method of reducing the non-linearities. For example let the original data output at a rate of 400 Hz and if the data is averaged for eight samples. Therefore the output rate would be $400 \mathrm{~Hz} / 8=50 \mathrm{~Hz}$.

### 5.4 Differential drive motor control (While traveling)

There could still be deviation of the actual trajectory when the robot is traveling, even though initial calibration as in section 5.1. This is analogous to a situation whereby when a person is driving a car with the steering wheel set such that the car moves in a straight direction. The person just sits there without holding the steering wheel while the car is in motion. After some time, the steering will move and the car moves side ways.

Therefore, some control algorithm is needed to sense that if one of the two motors move faster than the other the computer program will slow the faster moving motor down such that both of the speeds will be synchronised.

## Chapter 6: Motor Control

### 6.1 Pulse Width Modulation

PWM output is basically a series of pulses with varying size in pulse width. This PWM signal is output from the h-bridge circuit to control the wiper motor. The difference in pulse length shows the different output of h -bridge circuit controlling the output speed of the motor.


Figure 25: Pulse Width Modulation waveform
Figure above shows the varying pulse length of the pulse width modulation (PWM) scheme. Let's say that the PWM frequency is about 50 Hertz, with a period cycle of 20 ms . Therefore assuming that the T1 and T2 length values are 15 ms and 5 ms respectively, the duty cycle can be calculated as below:

$$
\begin{aligned}
\text { Duty cycle } & =\mathrm{T} 1 /(\mathrm{T} 1+\mathrm{T} 2) * 100 \% \\
& =15 / 20 * 100 \% \\
& =75 \%
\end{aligned}
$$

Therefore if the maximum rating speed of the wiper motor is about 1000 rpm , then the controlled speed would be 750 rpm .
If suddenly the h-bridge circuit wants to control the half the speed of the motor as in part 2 of figure (25) then the duty cycle value can be calculated as:

```
Duty cycle \(=\mathrm{T} 1 /(\mathrm{T} 1+\mathrm{T} 2) * 100 \%\)
    \(=10 / 20 * 100 \%\)
    \(=50 \% \quad\) Therefore the speed would be 500 rpm .
```


### 6.2 H-bridge design

### 6.2.1 Introduction

H-bridge circuit is a widely known circuit for controlling the direction spin and speed of DC motors. This is how the H -bridge circuit works. Let's denote one rotation is clockwise and the other direction spins as counter clockwise. Basically, the circuit consists of two p-channel MOSFETS (A \& B) and two N-channel (C \& D) MOSFETS. In order to turn the motor clockwise, the MOSFETS A and D are turn on while MOSFETS B and C are turn off at one instant. The same goes for counter clockwise direction whereby MOSFETS B and C are turn on while the MOSFETS A and D are turn off. This is best illustrated in the figures below.

## Step 1: Motor clockwise turn



Figure 26: Motor clockwise turn
$\rightarrow$ Current flowing clockwise $\quad \rightarrow$ CEMF current
When the motor starts to turn clockwise, the current will flow as above figure.

## Step 2: CEMF current flow



Figure 27: CEMF current flow

If the motor stops and starts to turn the other direction, which is counter-clockwise the opposite CEMF current will flow subsequently as above (Dennis Clark, pg191) . As can be seen the freewheeling diodes serves to protect the MOSFETS from being damage by the CEMF current. That is why there is a tendency that one vertical parallel 'leg' shorting when the motor starts to turn the motor the other direction immediately. This is not an ideal situation as it will damage the parallel MOSFETS. Therefore some delay time is needed to allow the CEMF current to finish flowing before starting the counter-clockwise turn as shown in figure 28.

## Step 3: Motor counter-clockwise turn



Figure 28: Motor counter clockwise turn

### 6.3 Design consideration

## Design consideration 1: Free-wheeling diodes

Dc motors are very powerful motors and because of that the motors can be term as powerful inductors. Inductors in nature tend to resist change in current. When turning off an inductor, current will gradually go to zero. However, the inductor will try to keep the current flowing. If the current is goes to zero faster, the harder the inductor will try to keep the current. This means current may shoot up higher thus resulting in high voltage across the inductor. The voltage, termed Counter Electro Motive Force (CEMF) is undesirable for the switching transistors which may in the end malfunction.

Since there is CEMF voltage there will also be CEMF current flowing in the transistors. Therefore clamping diodes ( 4 of them) are inserted as shown in figure. Instead of flowing into the transistors the will flow along the diodes path to ground. The clamping diodes can help limit the amount of high CEMF voltages to a low and desirable 0.3 to 0.7 volts.

## Design consideration 2: Transistors or MOSFET

Consider the motor operate at 12 V is about 2 A . The value 2 A can be compared with the rated drain current Id of MOSFET, which is 23 A and has as can be seen, has lots of tolerance so that it will not overheat.

## Design consideration 3: Opto-isolator

Opto-isolator is being considered here for high current design. This is to completely isolate circuitry of the microcontroller from the noisy motor circuitry. It is also used to switch the gate of a MOSFET on and off. The important characteristics of the Optoisolator is the fast rise and fall times. This is to make sure that the MOSFET is fully switched on fast. The below calculation can be used to check whether an opto-isolator is suitable for an application.

Let's say that the wanted PWM frequency is 50 Hz , therefore the period $=1 /$ Freq $=$ 20ms
$10 \%$ duty cycle $=20 \mathrm{~ms} * 0.1=2 \mathrm{~ms}$
$100 \%$ duty cycle $=20 \mathrm{~ms} * 1=20 \mathrm{~ms}$
Given the specification from the opto-isolator 4 n 26 (used in this project):
Turn on time $=10$ us
Turn off time $=10$ us
Total delays $=20 \mathrm{us}$
Therefore, since the total delays of the opto-isolator is able to switch on and off the MOSFETS fully and is suitable for use.

## Design consideration 4: totem pole transistor as MOSFET driver

This is normally used for driving and switching along with the MOSFET. The transistor considered is the fast switching transistor which is the 2N3904for NPN and 2N3906 for PNP.

### 6.4 Totem-pole circuit



Figure 29: Totem-pole and P-channel Mosfet

| N- Channel Mosfet | OFF | ON | BUZ10 |
| :---: | :---: | :---: | :---: |
| P- Channel Mosfet | ON | OFF | MT8 |
| Totem-pole | T1-ON,T2-OFF | T2-OFF,T2-ON | T1-NPN 2N3904 |
|  |  |  | T2- PNP 2N3906 |
| Optoisolator | ON | OFF | 4N26 |
|  |  |  |  |

Table 3: H-bridge circuit components operation
'high' $-5 \mathrm{~V} / 12 \mathrm{~V}$, 'low' -0 V

From the above configuration the P-channel MOSFET will conduct or turn on when the opto-isolator outputs a 'high' signal, which then turn on the transistor T1 and the transistor T2 will then automatically switches off.

Meanwhile, the N-channel MOSFET will turn on when the opto-isolator outputs a 'low' signal. This signal will then turn off the transistor T1 and the transistor T2 will then switch on. As can be observed, when the N-channel MOSFET is turn on, the Pchannel MOSFET turns off and vice-versa.

| P-channel MOSFET <br> $\mathrm{Vg}=0 \mathrm{~V}, \mathrm{Vs}=12 \mathrm{~V}$ | ON $(\mathrm{Vgs}=0 \mathrm{~V})$ | OFF $(\mathrm{Vgs}=12 \mathrm{~V})$ |
| :--- | :--- | :--- |
| $\mathrm{N}-\mathrm{channel} \mathrm{MOSET}$ <br> $\mathrm{Vg}=12 \mathrm{~V}, \mathrm{Vs}=0 \mathrm{~V}$ | $\mathrm{ON}(\mathrm{Vgs}=12 \mathrm{~V})$ | OFF $(\mathrm{Vgs}=0 \mathrm{~V})$ |

Table 4: MOSFET's operation
The operations of MOSFETs are summarised as above table 4.

### 6.5 Unwanted situation

Referring to the figure 29 above MOSFET B and D should not turn on at the same time.
Even though the programmer can program exactly such that only MOSFET A and D turn on and MOSFET B and C turn off there is a possibility that the MOSFET will fail in two situations below:
i) MOSFET does not turn on and off properly.
ii) MOSFET does not turn on and off fast enough.

### 6.6 Experiment

Bread boarding one n and p channel MOSFET circuit to test whether can turn the motor on or off. This experiment is also to determine which PWM frequency signal that can be used to drive the motor. Appropriate frequency is needed such that motor shaft would turn on smoothly without any jerky movement. In other words, the frequency must not be too low.

The MOSFET gate input is measured using oscilloscope to note whether pulse train shape is formed.


Figure 30: N-channel MOSFET motor driver

### 6.7 Results

### 6.7.1 Pulse Train



The left hand side photo indicates the pulses output from the microcontroller pin.

Voltage/div $=2.5$ volts
Time $/$ div $=10 \mathrm{~ms}$

Figure 31: Pulse train waveform

### 6.7.2 Current Surge

During the operation of the wiper motors there is a current surge whenever the motor starts to turn. Instead of the usual pulse waveform voltage spikes can be seen as 4 division space high. This is the motor running at rated 12 v without gearing down. Imagine what would happen if the motor is geared down such as the ratio of 3 . Current would shoot up three times higher. This would seriously damage the h -bridge circuit. Therefore, it is suggested that the voltage is ramped up to the voltage required within the short period of time such as 500 ms .

### 6.7.3 Noise isolation



Photo on the left shows the cleaner pulse train on the microcontroller circuitry.

Figure 32: Clean pulse train waveform


Figure 33: Noise corrupted pulse train waveform

## Chapter 7: Microcontroller \& Software

The type of microcontroller used is the PIC 16F877A that can be bought from microchip website www.microchip.com. The diagram of the microcontroller is as shown below:


Figure 34: Microcontroller schematic diagram
(Source: PIC16F877A, Microchip)

The table below some of the important features of the PIC16F877A

| Key Features PICmicro ${ }^{\text {TM }}$ Mid-Range Reference Manual (DS33023) | PIC16F873 | PIC16F874 | PIC16F876 | PIC16F877 |
| :---: | :---: | :---: | :---: | :---: |
| Operating Frequency | DC - 20 MHz | DC - 20 MHz | DC - 20 MHz | DC - 20 MHz |
| RESETS (and Delays) | POR, BOR (PWRT, OST) | $\begin{gathered} \text { POR, BOR } \\ \text { (PWRT, OST) } \end{gathered}$ | POR, BOR (PWRT, OST) | POR, BOR (PWRT, OST) |
| FLASH Program Memory (14-bit words) | 4K | 4K | 8K | 8K |
| Data Memory (bytes) | 192 | 192 | 368 | 368 |
| EEPROM Data Memory | 128 | 128 | 256 | 256 |
| Interrupts | 13 | 14 | 13 | 14 |
| I/O Ports | Ports A,B,C | Ports A,B,C,D,E | Ports A,B,C | Ports A,B,C,D,E |
| Timers | 3 | 3 | 3 | 3 |
| Capture/Compare/PWM Modules | 2 | 2 | 2 | 2 |
| Serial Communications | MSSP, USART | MSSP, USART | MSSP, USART | MSSP, USART |
| Parallel Communications | - | PSP | - | PSP |
| 10-bit Analog-to-Digital Module | 5 input channels | 8 input channels | 5 input channels | 8 input channels |
| Instruction Set | 35 instructions | 35 instructions | 35 instructions | 35 instructions |

Table 5: Comparison of microcontroller features
(Source: PIC 16F877A, Microchip)

### 7.1 Reasons

Reasons why PIC16F877A is chosen:
i) Many input output ports to choose from -5 all together
ii) Huge memory space - Nearly four hundred bytes
iii) Has Analog to Digital modules to convert analog voltage (from sensors) to digital value.
iv) Interrupt feature

This function is very useful in programming as it enables two programs running at the same time, with one running in the background. When one of the programs is of higher priority and after some time the microcontroller for instance will service the higher priority program first and later return the handling to the other lower priority program.

### 7.2 Memory



Figure 35: Microcontroller memory (Source: PIC16F877A, Microchip)

PIC microcontrollers have two separate blocks of memory. One of them is the program memory and memory for file registers (PIC16F877A, Microchip). The program memory shown in the figure above represents the total amounts of program programmable into the PIC16F877. While the memory for file registers is the address for built-in registers. (i.e: STATUS, OPTION_REG) (PIC16F877A, Microchip).

### 7.3 Time consideration

### 7.3.1 Oscillators

There are four different types of clock oscillators that can be used with the PIC microcontroller. It is listed as follows:
a) RC - resistor/capacitor
b) XT - crystal or ceramic resonator
c) HS - high speed crystal or ceramic resonator
d) LP - low power crystal

The crystal or ceramic resonator is used because it is accurate and reliable. An example value for this crystal oscillator is 4 MHz .

Although the time to process one cycle looks like $1 / 4 \times 10^{\wedge} 6=0.25$ us it is actually not. The actual time for the processor to execute one instruction cycle is 1 us. In other words, executing each instruction line takes 1us.

This is because the processor needs to undergo a few stages in order to successfully execute one machine cycle. They are fetch, decode, execute and store.

### 7.4 Software

One of the advantages of using the assembly program (MPLAB) is that the user gets to know in detail how much time used for every cycle executed.


Figure 36: MPLAB interface program

### 7.5 Arithmetic Operation

Arithmetic Operation in assembly is different from what is used in high level language such as C . The four types of operations are shown and work out below. There will be a comparison of the C language and the respective addition, subtraction, multiplication and division.

The main difference is that programming is C is easier. However, by programming in assembly language a person can get to know how the computer operates the arithmetic operations.

## Subtraction in C

Answer $=280-8=272$

## Subtraction in Assembly

$$
0000000100011000
$$

- 0000000000001000
$0000000100010000 \quad(=272)$

Multiplication in C
Answer $=16 * 150=2400$

## Multiplication in assembly

Assuming the multiplication in the $150 * 16$
$\mathrm{W}=16$ (00010000)
$\mathrm{Lo}=150$ (10010110)

```
Rrf hi&lo (00000000 X1001011), Carry = 0
(answer:0)
No carry
Rrf hi & lo (00000000 0X100101), Carry =1
(answer:0)
carry! Hi+w (=00100101)
Rrf hi & lo (00010010 10X10010), Carry = 1
(answer:16*2=32)
carry! Hi+w (=10110111)
Rrf hi & lo (01011011 110X1001), Carry = 0
(answer:16*2+16*4= 96)
no carry
Rrf hi & lo (00101101 1110X100), Carry = 1
(answer:0)
carry! Hi+w =(00010001)
Rrf hi & lo (00001000 11110X10), Carry=0
(answer: 16*2+16*4+ 16*16=352)
No carry
Rrf hi & lo (00000100 011110X1), Carry =0
No Carry
Rrf hi \& lo ( 00000010 0011110X), Carry \(=1\)
Carry! Hi+w (=00111110)
Rrf hi \& lo ( 0001111100000000 ), Carry=X
(answer: \(16 * 2+16 * 4+16 * 16+16 * 128=2400\) )
```

In assembly it is just shifting the registers of 150 ( 8 bit) value in 9 times and multiply the result as shown above. Values with more than 255 ( 8 bit) can also be done the similar way as above. It is just that have to shift 17 times and multiply.

Full program listing is in the appendix D.

### 7.5.1 Trade-off

There are two major trade-offs that the programmer might face in using the assembly language. One is the level of tediousness. Programming the arithmetic operations can be time consuming and difficult to check for errors.

Secondly, it is the level of accurateness. It is not accurate to use the above simple methods to calculate the floating point (or decimal point). Any results that has decimal point the program will round them up and output integer values.

## Chapter 8: PCB design consideration

There are several rules to be followed in designing a Printed Circuit Board (PCB). This is to make sure that the circuit to be created works properly by not having it affected by any unwanted interference (i.e noise) or current (in Amperes) free-flowing without any obstruction.

The main considerations are:

## i) Components Arrangements

Components are arranged uniformly parallel or 90 degrees to each other.

## ii) Conductor width

The copper tracks on the circuit board use the suitable track width. The current flow through the tracks is the main consideration. The higher current needed to flow the wider
track width is needed. (Electronic Measurement Workbook, USQ)

## iii) Conductor length

Conductor's connection from one point to another should be as short as possible. The longer the conductor length the more disadvantage to the circuit be. This is because longer conductor length will act a transmission lines, which is susceptible to interference and noises from the external environment.( Electronic Measurement Workbook, USQ)

## iv) Pad sizes

There is a standard rule of thumb the pad sizes should be about 2 to 2.5 times the diameter of the hole.

The designs for the microcontroller, accelerometer and h-bridge circuit boards are attached in the appendix B

## Chapter 9: Discussion \& Conclusion

### 9.1 Results

There are a few experiments that are tried and tested. It is as follows:

### 9.1.1 Gyro mounting

When testing the gyro at the laboratory the gyro exhibits a fast response. For instance, the faster the gyro rotates the faster the reading being output. Due to the fact that the gyro measures the rate of turn, and when the gyro stay still the gyro will output a steady state reading, which is 3.0 V . Initially, the motor buzzing and after a while it keeps buzzing.

### 9.1.2 Accelerometer

In the experiment with the accelerometer alone the robot could not balance. There is a possibility that the response time is slow and could not output the signal to the motors to turn.

### 9.2 Reasons

The robot does not manage to balance by itself. There might be a few reasons for this.

## i) Unsuitable Control

The control might be too simplistic even though the control strategy seems logical at. first. This issue is not realised initially as the programming language used in assembly

## ii) Does not provide the actual angle

As for the gyro as the sensor and it might not be too good in directly reading the values. Instead, we could try in adding an integrator block in whereby after integration the angular rate data would become the angular data. With this, the accelerometer might not be needed. This could be done in assembly such that when the time the robot takes to tilt the microcontroller is used to record the time and subsequently control the robot by lifting the chassis back up in the amount of time.

## iii) Programming skill

There is a possibility that the programming skill may not up to the mark since this is the first time such a tedious program is being written.

### 9.3 Incomplete tasks

### 9.3.1 Gyro-Accelerometer Combo

Due to the time constrains this experiment is not able to be executed even though the program is already written. More time is needed to troubleshoot. If this problem is fixed then theoretically the user might get the robot balance more stable.

### 9.4 Conclusion

### 9.4.1 Recommendation for Future Work

Researchers could build on what is researched until now. There are a few experiments that are unaccomplished. That is the main drawback that hampers the overall project as concrete results is unable to attain. Therefore appropriate conclusions are not able to achieve.

Programming in assembly is tedious and time consuming. Even a slightest error may result in whole program could not work. Detecting the mistake is hard as there are so many lines of commands. Therefore, in future researchers might want to switch to C programming for future research and development.

## References

Anderson, D.P, 'Nbot, a two wheel balancing robot', Viewed 28 February 2005 [http://www.geology.smu.edu/~dpa-www/robo/nbot](http://www.geology.smu.edu/~dpa-www/robo/nbot)

Steve Hassenplug, 2002, 'Steve’s Legway’, Viewed 4 March 2005
[http://www.teamhassenplug.org/robots/legway/](http://www.teamhassenplug.org/robots/legway/)
Dean Kamen ,2001, Viewed 7 March 2005
[http://www.segway.com](http://www.segway.com)
John Green, David Krakauer, March 2003, New iMEMS Angular Rate Sensing Gyroscope, Viewed 12 April 2005, [http://www.analog.com/library/analogDialogue/archives/37-03/gyro.html](http://www.analog.com/library/analogDialogue/archives/37-03/gyro.html)

Peter Hemsley, 32-bit signed integer maths for PICS, Viewed 2 April 2005 [http://www.piclist.com/techref/microchip/math/32bmath-ph.htm](http://www.piclist.com/techref/microchip/math/32bmath-ph.htm)

30 Jan2002, Mosfets and Mosfet's drivers, [http://homepages.which.net/~paul.hills/SpeedControl/Mosfets.html](http://homepages.which.net/~paul.hills/SpeedControl/Mosfets.html)

Rick Bickle, 11 July 2003, 'DC motor control systems for robot applications', Viewed 15 April [http://www.dprg.org/tutorials/2003-10a/motorcontrol.pdf](http://www.dprg.org/tutorials/2003-10a/motorcontrol.pdf)

Carnegie Mellon, 26 August 1997, 'Control Tutorials for Matlab', The University of Michingan, Viewed 25 February 2005
[http://www.engin.umich.edu/group/ctm/PID/PID.html](http://www.engin.umich.edu/group/ctm/PID/PID.html)
[http://www.boondog.com/tutorials/mouse/mouseHack.htm](http://www.boondog.com/tutorials/mouse/mouseHack.htm)
Martin Rowe, 11 January 2001, Measuring PWM motor efficiency, Test \& Measurement World, Viewed 14 April 2005
<http://www.reed-electronics.com/tmworld/article/CA180848.html >
Gerry, 6 Ferbruary, Tilt sensors for your Robot, Viewed 2 March 2005
[http://www.roboticsindia.com/modules.php?name=News\&file=article\&sid=90](http://www.roboticsindia.com/modules.php?name=News%5C&file=article%5C&sid=90)
(c) 1998, 2001 EME Systems, Berkeley CA U.S.A., Pulse Width Modulation, Viewed 29 February 2005
[http://www.emesystems.com/BS2PWM.htm](http://www.emesystems.com/BS2PWM.htm)

2001 Microchip Technology Inc, PIC 16F87X data sheet, Viewed 14 February 2005 <www.microchip.com>

2004 Analog Devices, Inc, All rights reserved, ADXLS213, viewed 15 February 2005 <www.analogdevices.com>

2004 Analog Devices, Inc, All rights reserved, ADXRS300, viewed 15 February 2005 <www.analogdevices.com>

David Bension, version 4, Easy Microcontrol'n, A Beginners' guide to using PIC Microcontrollers, Square 1.

Dennis Clark and Michael Owings, 'Building Robot Drive Trains', McGraw Hill Companies.
D.W.Smith, 2002, PIC in Practice, Newnes, An imprint of Elsevier Science

Naoji Shiroma, Osamu Matsumoto, Shuji Kajita, Kazuo Tani, ‘Cooperative Behavior of a Wheeled Inverted Pendulum for Object Transportation', Proceedings of the 1996 IEEE/RSJ International conference on Intelligent Robots and Systems '96, IROS 96, volume:2, 4-8Nov. $1996 \mathrm{Pg}(\mathrm{s}): 396-401$ vol.

Grasser, Felix, Alonso D’Arrigo, Silvio Colombi \& Alfred C. Rufer, 2002, 'JOE: A Mobile, Inverted Pendulum', IEEE Transactions on Industrial Electronics, vol 49.

Young Soo Suh, 'Attitude Estimation using Low Cost Accelerometer and Gyroscope’, Proceedings of the $7^{\text {th }}$ Korea-Russia International Symposium, KORUS 2003, $\operatorname{Pg}(\mathrm{s})$ 423-427.

Albert-Jan Baervaeldt and Robert Klang, 'A Low-cost and Low-weight Attitude Estimation System for an Autonomous Helicopter', Halmstad University, Sweden, $\operatorname{Pg}(\mathrm{s})$ 391-395.

Yongjun Hou, Greg R.Luecke, October 5-8 2003, ‘Control of the Tight Rope Balancing Robot', Proceedings of the 2003 IEEE International Symposium on Intelligent Control, Houston, Texas, Pg(s): 896-901.

Alessio Salerno and Jorge Angles, 'The Control of Semi-Autonomous Two-Wheeled Robots Undergoing Large Payload-Variations', Proceedings of the 2004 IEEE International Conference on Robotics \& Automation, New Orleans, LA, Pg(s): 17401745.

Kiyoshi Komoriya and Eimei Oyama, 'Position Estimation of a Mobile Robot Using Optical Fiber Gyroscope (OFG)’, $\operatorname{Pg}(\mathrm{s}):$ 143-149.

Prof. John Billingsley, Mechatronics Practice Unit, Viewed 11 May 2005
[http://www.usq.edu.au/course/material/eng3905/](http://www.usq.edu.au/course/material/eng3905/)

Dr.Tony Ah Fock, Power Electronics study book 1 and 2, University of Southern Queensland.

Paul E.Sandin , "Robot Mechanisms and Mechanical Devices Illustrated", The McGrawHill companies.
J.J. D’Azzo, C.H. Houpis, Feedback Control System Analysis and Synthesis, second edition, McGraw-Hill International Editions. (ISBN 0-07-Y85150-6) Pg11
'Inverted Pendulum', Microrobot NA, Viewed 27 February 2005
http://www.microrobotna.com/pendulum.htm
R.E Kalman, 1960, 'A New Approach to Linear Filtering and Prediction Problems', Transactions of the ASME- Journal of Basic Engineering, 82(Series D), pp35-45.

## Appendix A: Project Specification

# FACULTY OF ENGINEERING AND SURVEYING 

## ENG4111/4112 Research Project PROJECT SPECIFICATION

FOR: HO, KHOON CHYE (RANDAL)
TOPIC: BALANCING WHEELED ROBOT
SUPERVISORS: Mr. Mark Phythian (USQ)
Dr. Izham Bin Zainal Abidin (Uniten, Malaysia)
ENROLMENT: ENG4111-S1, XP, 2005
ENG4112-S2, XP, 2005
PROJECT AIM: This project aim is to build a robot that can balance itself on two wheels without falling.

SPONSORSHIP: Individual / USQ
PROGRAMME: Issue A, 21 March 2005

1. Research information on designing a two wheel balancing robot by identifying the type of programming software to use and selecting control methods to be applied on the robot.
2. Design and assemble two-wheel robot base.
3. Understand, write and troubleshoot MATLAB programming software on determining the behavior of robot and torque needed by motor to balance the robot in the upright position.
4. Analyze and understand the process flow of the motor and chassis controlling program.
5. Write and troubleshoot PIC programming software on the controlling of motor and chassis of robot.
6. Design Printed Circuit Board for motor controller and sensors.
7. Evaluate the performance of balancing robot by implementing two types of sensors.

As time permits:
8. Add and design extra feature for the robot that can follow lines while traveling.

## AGREED:

$\qquad$
(dated) $\qquad$

## Appendix B

## Source Codes

## Accelerometer Acquisition program (MPLAB)

List $\mathrm{p}=16 \mathrm{~F} 877 \mathrm{a}$
include "p16f877a.inc"
__config _cp_off \& _wdt_off \& _xt_osc \& _pwrte_on
;Reading Accelerometer duty cycle value
;This subroutine collects and calculates T1X, T1Y and T2
;T1X is represented by registers T1 XHi and T1Xlo
; T1 Y is represented by registers T1 YHi and T1Ylo
;T2 is represented by registers T 2 Hi and T 2 lo

| T1XEndlo | equ | 46 h |
| :--- | :--- | :--- |
| T1XEndHi | equ | 47 h |
| T1Ybeginlo | equ | 48 h |
| T1YbeginHi | equ | 49 h |
| T1YEndlo | equ | 50 h |
| T1YEndHi | equ | 55 h |
| T1YHi | equ | 56 h |
| T1YLo | equ | 81 h |
| T1XHi | equ | 82 h |
| T1XLo | equ | 83 h |
| T2Hi | equ | 85 h |
| T2Lo | equ | 86 h |
| ZXcalHi | equ | 87 h |
| ZXcalLo | equ | 88 h |
| ZXActualHi | equ | 89 h |
| ZXActualLo | equ | 95 h |
| u_term_lo_acce | equ | 96 h |
| u_term_hi_acce | equ | 97 h |
| KHi | equ | 98 h |
| KLo |  |  |

- Start at the reset vector
org 0x000
goto start
org 0x0004

incf
bcf
bcf

retfie $\quad$|  |
| :--- | :--- |

Start

| bcf | STATUS,RP0 |  |  |
| :--- | :--- | :--- | :--- |
| clrf | PORTA |  |  |
| clrf | PORTB |  | ;Bank1 |
| bsf | STATUS,RP0 |  |  |
| movlw | B'00000011' | ;Set up the I/O ports |  |
| movwf | TRISA |  |  |
| movlw | B'00010000' |  |  |
| movwf | TRISB |  |  |
| movlw | B'00001111, |  |  |
| movwf | OPTION_REG |  |  |
| bcf | STATUS,RP0 |  |  |
| bsf | INTCON,GIE |  |  |
|  |  |  |  |
| Movlw | b'00100011' |  |  |
| Movwf | T1CON |  |  |
| Movlw | b'00000101' |  |  |
| Movwf | CCP1 |  |  |
| bsf | INTCON,GIE |  |  |


| EdgeA | btfsc <br> Goto | PORTA,0 <br> EdgeA |
| :--- | :--- | :--- |
| EdgeB | btfss | PORTA,0 |$\quad$;Look for the high transmission at

EdgeD btfsc PORTB,2
goto EdgeD
EdgeE btfsc PORTB,2 ;Look for the high transmission at Tc
Goto EdgeE ;Keep looking for high transmission

Movf TMR1L,w ;Record and save the time in T1 Ybeginlo Movwf T1Ybeginlo
Movf TMR1H,w
Movwf T1YbeginHi
EdgeF
btfsc PORTB,2 ;Look for the low transmission at
Td
Goto EdgeF ;Keep looking for low transmission
Movf TMR1L,w ;Record and save the time in
Movwf T1 YEndlo ; T1 YEndlo
Movf TMR1H,w
Movwf T1YEndHi
Movf T1YEndHi,w
Movwf Arg_hi
Movf T1YEndlo,w
Movwf Arg_lo
Movf T1YbeginHi,w
Movwf Sum_Hi
Movf T1YbeginLo,w
Movwf Sum_Lo
call Subtract
Movf Sum_Hi,w
Movwf T1YHi
Movf Sum_Lo,w
Movwf T1YLo
;CALCULATE T2
;2*(T2Hi,T2Lo) = (T1YEndHi:T1YEndLo) +
;(T1YStartHi:T1 YStartLo)-(T1XHi:T1XLo)

| movf | T1YEndHi,w |
| :--- | :--- |
| movwf | Arg_Hi |
| movf | T1YEndLo,w |
| movwf | Arg_Lo |
| movf | T1YbeginHi,w |
| movwf | Sum_Hi |
| movf | T1YbeginLo,w |
| movwf | Sum_lo |
| call | add |

;Sum_hi,Sum_lo=(T1YEndHi:T1YEendLo)+
movf T1XEndHi,w ;
(T1YBeginHi:T1YBeginLo)
movwf Sum_Hi
movf T1XEndLo,W

; The x -axis acceleration value is programmed based on the formula
; Acceleration $=\mathrm{K}^{*}(\mathrm{~T} 1-$ Zactual $) / T 2$ actual

| X_Accel_value | movf <br> Subwf <br> Btfss <br> Goto <br> Btfss | ZXActualHi,w $;$ This is to check whether the <br> T1XHi,w <br> STATUS,c numerator is positive or negative |
| :--- | :--- | :--- |


| Goto | Num_posx |
| :--- | :--- |
| Movf | ZXActualLo,w |
| Subwf | T1XLo,w |
| Btfss | STATUS,c |
| Goto | Num_posx |

;This subroutine is chosen if the x -axis acceleration value is negative

| Num_negx | movf <br> Movwf <br> Movf <br> Movwf <br> Movf <br> Movwf <br> Movf <br> Movwf <br> Call <br> Movlw <br> Movwf <br> Movlw <br> Mowwf <br> Call | ZXActualHi,w <br> Arg_Hi <br> ZXActualLo,w <br> Arg_Lo <br> T1XHi,w <br> Sum_hi <br> T1XLo, w <br> Sum_lo <br> Subtract <br> KHi <br> Arg_Hi <br> KLo <br> Arg_Lo <br> Mul |
| :---: | :---: | :---: |
|  | Movf <br> Movwf <br> Movf <br> Movwf <br> Call | T2Hi,w <br> Divisor 1 <br> T2Lo,w <br> Divisor0 <br> Division |
|  | Movf <br> Movwf <br> Movf <br> Movwf <br> Call <br> movf <br> movwf <br> movf <br> movwf | T2Hi,w <br> Divisor 1 <br> T2Lo,w <br> Divisor0 <br> Division <br> Quo_0,w <br> u_term_hi_acce <br> Quo_1,w <br> u_term_lo_acce |
|  | $\begin{aligned} & \text { movf } \\ & \text { sublw } \\ & \text { call } \\ & \text { movwf } \\ & \text { btfsc } \\ & \text { call } \\ & \text { call } \end{aligned}$ | u_term_hi_acce,w <br> b'00000010' ; Upper byte for analog value 3 V <br> no_drive <br> temp_lo <br> STATUS, c <br> ccw <br> cw |


| no_drive | movwf <br> btfsc <br> call <br> return | temp_lo <br> STATUS,z <br> next_byte3 |
| :--- | :--- | :--- | ;No Signal is output to the h-bridge

;This section is to determine which direction the motor should turn next_byte3

|  | bcf | STATUS, c |  |
| :---: | :---: | :---: | :---: |
|  | bcf | STATUS,z |  |
|  | bsf | STATUS,RP0 |  |
|  | movf | u_term_lo_acce |  |
|  | bcf | STATUS,RP0 |  |
|  | sublw | b'00000001' | ;lower byte for analog value 3V |
|  | call | no_drive_test2 | ;This is the balanced state value |
|  | btfsc | STATUS, c |  |
|  | call | ccw | ;If no carry then go to ccw |
| subroutine |  |  |  |
|  | call | cw | ;If carry then go to cw subroutine |
| no_drive_test2 | movwf | temp_lo |  |
|  | btfsc | STATUS,z |  |
|  | call | clr_drive | ;No Signal is output to the h-bridge |

;This ccw subroutine contains a few individual error values, which in turn will call the ;appropriate duty cycle subroutines.

|  | movf <br> sublw <br> btfsc <br> call | $\begin{aligned} & \text { u_term_hi_acce,w } \\ & \text { b'00000000' ; upper byte error value }(3-1.8) v \\ & \text { STATUS,z } \\ & \text { upper_byte } \end{aligned}$ |
| :---: | :---: | :---: |
| valtest1 | movf | u_term_hi_acce, w |
|  | sublw | $\mathrm{b}^{\prime} 00000000{ }^{\prime}$; upper byte error value (3-1.9)v |
|  | movwf | test_bytelo |
|  | btfsc | STATUS,z |
|  | call | upper_byte2 |
|  | movwf | test_bytelo |
|  | btfss | STATUS, c |
|  | call | set_cycle1 |


| valtest2 | movf <br> sublw <br> movwf <br> btfsc <br> call <br> movwf btfss <br> call | u_term_hi_acce,w <br> b'00000000' ; upper byte error value (3-2)v <br> test_bytelo <br> STATUS,z <br> upper_byte3 <br> test_bytelo <br> STATUS, c <br> set_cycle2 |
| :---: | :---: | :---: |
| valtest3 | movf <br> sublw <br> movwf <br> btfsc <br> call <br> movwf <br> btfss <br> call | ```u_term_hi_acce,w b'00000000' ; upper byte error value (3-2.1)v test_bytelo STATUS,z upper_byte4 test_bytelo STATUS,c set_cycle3``` |
| valtest4 | movf <br> sublw <br> movwf <br> btfsc <br> call <br> movwf <br> btfss <br> call | ```u_term_hi_acce,w b'00000000' ; upper byte error value(3-2.2)v test_bytelo STATUS,z upper_byte5 test_bytelo STATUS,c set_cycle4``` |
| valtest5 | movf <br> sublw <br> movwf <br> btfsc <br> call <br> movwf <br> btfss <br> call | ```u_term_hi_acce,w b'00000000' ; upper byte error value (3-2.3)v test_bytelo STATUS,z upper_byte6 test_bytelo STATUS,c set_cycle5``` |
| valtest6 | movf <br> sublw <br> movwf <br> btfsc | u_term_hi_acce,w <br> b'00000000' ; upper byte error value (3-2.4)v test_bytelo <br> STATUS, z |


|  | call <br> movwf <br> btfss <br> call | upper_byte7 <br> test_bytelo <br> STATUS, c <br> set_cycle6 |
| :---: | :---: | :---: |
| valtest7 | movf <br> sublw <br> movwf <br> btfsc <br> call <br> movwf <br> btfss <br> call | u_term_hi_acce,w <br> $\mathrm{b}^{\prime} 00000000$ ' ; upper byte error value (3-2.5)v <br> test_bytelo <br> STATUS, z <br> upper_byte8 <br> test_bytelo <br> STATUS, c <br> set_cycle7 |
| valtest8 | movf <br> sublw <br> movwf <br> btfsc <br> call <br> movwf <br> btfss <br> call | u_term_hi_acce,w <br> $\mathrm{b}^{\prime} 00000000$ ' ; upper byte error value (3-2.6)v <br> test_bytelo <br> STATUS,z <br> upper_byte9 <br> test_bytelo <br> STATUS, c <br> set_cycle8 |
| valtest9 | movf <br> sublw <br> movwf <br> btfsc <br> call <br> movwf <br> btfss <br> call | ```u_term_hi_acce,w b'00000000' ; upper byte error value (3-2.7)v test_bytelo STATUS,z upper_byte8 test_bytelo STATUS,c set_cycle9``` |
| valtest10 | movf <br> sublw <br> movwf <br> btfsc <br> call <br> movwf <br> btfss <br> call | ```u_term_hi_acce,w \(\mathrm{b}^{\prime} 00000000\) ' ; upper byte error value (3-2.8)v test_bytelo STATUS,z upper_byte9 test_bytelo STATUS, c set_cycle10``` |
| valtest11 | movf <br> sublw <br> movwf <br> btfsc <br> call | u_term_hi_acce,w <br> $\mathrm{b}^{\prime} 00000000$ ' ; upper byte error value (3-2.9)v <br> test_bytelo <br> STATUS,z <br> upper_byte10 |


|  | movwf <br> btfss <br> call <br> call | test_bytelo <br> STATUS, c <br> set_cycle11 <br> clr_drive |
| :---: | :---: | :---: |
| upper_byte | movf <br> sublw <br> movwf <br> btfss <br> call | ```u_term_lo_acce,w b'11110110' ; lower byte error value (3-1.8)v test_bytelo STATUS,c set_cycle1``` |
| upper_byte2 | movf <br> sublw <br> movwf <br> btfss <br> call <br> call | u_term_lo_acce,w <br> b'11100010' ; lower byte error value ( $3-1.9$ ) v <br> test_bytehi <br> STATUS, c <br> set_cycle1 <br> valtest2 |
| upper_byte3 | movf <br> sublw <br> movwf <br> btfss <br> call <br> call | $\begin{aligned} & \text { u_term_lo_acce,w } \\ & \text { b'11001101' ; lower byte error value }(3-2.0) \mathrm{v} \\ & \text { test_bytehi } \\ & \text { STATUS,c } \\ & \text { set_cycle2 } \\ & \text { valtest3 } \end{aligned}$ |
| upper_byte 4 | movf <br> sublw <br> movwf <br> btfss <br> call <br> call | $\begin{aligned} & \text { u_term_lo_acce,w } \\ & \text { b'10111001' }^{l} \quad ; \text { lower byte error value }(3-2.1) \mathrm{v} \\ & \text { test_bytehi } \\ & \text { STATUS,c } \\ & \text { set_cycle3 } \\ & \text { valtest } 4 \end{aligned}$ |
| upper_byte5 | movf <br> sublw <br> movwf <br> btfss <br> call <br> call | u_term_lo_acce,w <br> b'10100100' ; lower byte error value ( $3-2.2$ )v <br> test_bytehi <br> STATUS, c <br> set_cycle4 <br> valtest5 |
| upper_byte6 $2.3) \mathrm{v}$ | movf <br> sublw movwf btfss call | u_term_lo_acce,w ;lower byte error value (3- <br> b'10010000' <br> test_bytehi <br> STATUS, c <br> set_cycle5 |


|  | call | valtest6 |
| :--- | :--- | :--- |
| upper_byte7 |  |  |
| 2.4)v | movf | u_term_lo_acce,w ;lower byte error value (3- |
|  | sublw | b'01111011' $^{\text {movwf }}$ |
|  | test_bytehi |  |
|  | ctfss | STATUS,c |
|  | call | set_cycle6 |
|  | valtest7 |  |


| movwf | test_bytehi |
| :--- | :--- |
| btfss | STATUS,c |
| call | set_cycle11 |
| goto | $\$-1$ |

;The duty cycle values based on ON and OFF Pulse Width Modulation

| set_cycle1 | movlw | h'E5' | ; 100\% duty cycle |
| :---: | :---: | :---: | :---: |
|  | movwf | fr_cnt |  |
|  | movlw | h'FE' |  |
|  | movwf | fr_cnt2 |  |
|  | call | dir_chg |  |
|  | call | ramp_rou |  |
| set_cycle2 | movlw | $h^{\prime} \mathrm{E} 7^{\prime}$ | ;95\% duty cycle |
|  | movwf | fr_cnt |  |
|  | movlw | h'FD' |  |
|  | movwf | fr_cnt2 |  |
|  | call | dir_chg |  |
|  | call | ramp_rou |  |
| set_cycle3 | movlw | h'E8' | ; $90 \%$ duty cycle |
|  | movwf | fr_cnt |  |
|  | movlw | h'FC' |  |
|  | movwf | fr_cnt2 |  |
|  |  | dir_chg |  |
|  | call | ramp_rou |  |
| set_cycle4 | movlw | h'E9' | ; $85 \%$ duty cycle |
|  | movwf | fr_cnt |  |
|  | movlw | h'FB' |  |
|  | movwf | fr_cnt2 |  |
|  |  | dir_chg |  |
|  | call | ramp_rou |  |
| set_cycle5 | movlw | $\mathrm{h}^{\prime} \mathrm{EA}^{\prime}$ | ; $80 \%$ duty cycle |
|  | movwf | fr_cnt |  |
|  | movlw | h'FA' |  |
|  | movwf | fr_cnt2 |  |
|  | call | dir_chg |  |
|  | call | ramp_rou |  |
| set_cycle6 | movlw | $\mathrm{h}^{\prime} \mathrm{EC}^{\prime}$ | ;75\% duty cycle |
|  | movwf | fr_cnt |  |


|  | movlw <br> movwf <br> call <br> call | h'F9' <br> fr_cnt2 <br> dir_chg <br> ramp_rou |  |
| :---: | :---: | :---: | :---: |
| set_cycle7 | movlw <br> movwf <br> movlw <br> movwf <br> call <br> call | h'ED' <br> fr_cnt <br> h'F7' <br> fr_cnt2 <br> dir_chg <br> ramp_rou | ;70\% duty cycle |
| set_cycle8 | movlw <br> movwf <br> movlw <br> movwf <br> call <br> call | $h^{\prime} E E^{\prime}$ <br> fr_cnt <br> h'F6' <br> fr_cnt2 <br> dir_chg <br> ramp_rou | ;65\% duty cycle |
| set_cycle9 | movlw movwf movlw movwf call call | $h^{\prime} E F^{\prime}$ <br> fr_cnt <br> h'F5' <br> fr_cnt2 <br> dir_chg <br> ramp_rou | ; $60 \%$ duty cycle |
| set_cycle 10 | movlw <br> movwf <br> movlw <br> movwf <br> call <br> call | $h^{\prime}$ 'F1' <br> fr_cnt <br> h'F4' <br> fr_cnt2 <br> dir_chg <br> ramp_rou | ;55\% duty cycle |
| set_cycle 11 | movlw movwf movlw movwf call call | h'F2' <br> fr_cnt <br> h'F2' <br> fr_cnt2 <br> dir_chg <br> ramp_rou | ;50\% duty cycle |
| clr_drive | bcf bcf bcf bcf movlw movwf | PORTB, 5 <br> PORTB, 7 <br> PORTB, 1 <br> PORTB,2 <br> h'e5' <br> fr_cnt |  |


| call | delay1 |
| :--- | :--- |
| call | dir_chg2 |

; Time delay in ensuring the current is fully flowed to ground before
; Starting to turn the other direction of motor. This is to prevent short circuit from happening. The delay is about 500 ms

| dir_chg2 | movlw | h'FF' |
| :--- | :--- | :--- |
| Con2 | movwf | cnt4 |
|  | movlw | h'FF' |
|  | Movwf | cnt5 |
|  | decfsz | cnt5,1 |
|  | goto | $\$-1$ |
|  | decf | cnt4,1 |
|  | movf | cnt4,w |
|  | sublw | h'be' |
|  | btfss | status,z |
|  | goto | Con2 |
|  | incf | num_times |
|  | movf | num_times,w |
|  | subwf | fr_cnt1,w |
|  |  |  |
|  | btfss | status,z |
|  | goto | dir_chg2 |
|  | call | EdgeA |

;The other time delay for motor to turn the other direction. The function is same as above
;subroutine

| dir_chg | movlw | h'FF' $^{\prime}$ |
| :--- | :--- | :--- |
| Con3 | movwf | cnt4 |
|  | movlw | h'FF $^{\prime}$ |
|  | movwf | cnt5 |
|  | decfsz | cnt5,1 |
|  | goto | $\$-1$ |
|  | decf | cnt4,1 |
|  | movf | cnt4,w |
|  | sublw | h'be' |
|  | btfss | status,z |
|  | goto | Con3 |
|  | incf | num_times |
|  | movf | num_times,w |
|  | sublw | $d^{\prime} 20^{\prime}$ |


| btfss | status,z <br> goto <br> return |
| :--- | ---: |
| dir_chg |  |

; Thie Ramp_rou subroutine is to start the ramping up of motor voltage

| ramp_rou | movlw | h'fc' |
| :---: | :---: | :---: |
|  | movwf | ramp_cnt |
|  | movlw | h'ea' |
|  | movwf | ramp_cnt2 |
|  | call | PWM_ramp |
|  | decf | ramp_cnt |
|  | movf | fr_cnt,w |
|  | subwf | ramp_cnt, w |
|  | btfss | STATUS, c |
|  | call | PWMbegin |
|  | incf | ramp_cnt2 |
|  | call | PWM_ramp |
|  | goto | ramp_rou |
| PWM_ramp | bcf | PORTB, 7 |
|  | bsf | PORTB, 4 |
|  | call | delay1 |
|  | bcf | PORTB, 2 |
|  | bsf | PORTB, 1 |
|  | call | delay2 |
|  | bcf | PORTB, 7 |
|  | bcf | PORTB, 4 |
|  | call | delay1 |
|  | bcf | PORTB, 2 |
|  | bcf | PORTB, 1 |
|  | call | delay2 |
|  | return |  |

; Output the PWM signal to respective PORTS

| PWMbegin | bcf | PORTB,7 |
| :--- | :--- | :--- |
|  | bsf | PORTB,4 |
|  | call | delay1 |
|  | bcf | PORTB,2 |
|  | bsf | PORTB,1 |
|  | call | delay2 |
|  | bcf | PORTB,7 |
|  | bcf | PORTB,4 |
|  | call | delay1 |
|  | bcf | PORTB,2 |
|  | bcf | PORTB,1 |
|  | call | delay2 |


| incf | cnt3 |
| :--- | :--- |
| movf | cnt3,w |
| sublw | d'50' $^{\prime}$ |
| btfss | status,z |
| goto | PWMbegin |
| clrf | cnt3 |
| clrf | num_times |
| call | EdgeA |

;Below are the subroutines to select the appropriate duty cycle values based on the on and
;off time of pulses.

| set2_cycle 1 | movlw | h'E5' |
| :---: | :---: | :---: |
|  | movwf | fr_cnt |
|  | movlw | h'FE' |
|  | movwf | fr_cnt2 |
|  | call | dir_chg |
|  | call | ramp_rou |
| set2_cycle2 | movlw | $\mathrm{h}^{\prime} \mathrm{F}^{\prime}$ |
|  | movwf | fr_cnt |
|  | movlw | h'FD' |
|  | movwf | fr_cnt2 |
|  | call | dir_chg |
|  | call | ramp_rou |
| set2_cycle3 | movlw | h'E8' |
|  | movwf | fr_cnt |
|  | movlw | $\mathrm{h}^{\prime} \mathrm{FC}{ }^{\prime}$ |
|  | movwf | fr_cnt2 |
|  | call | dir_chg |
|  | call | ramp_rou |
| set2_cycle4 | movlw | $\mathrm{h}^{\prime} \mathrm{E} 9^{\prime}$ |
|  | movwf | fr_cnt |
|  | movlw | h'FB' |
|  | movwf | fr_cnt2 |
|  | call | dir_chg |
|  | call | ramp_rou |
| set2_cycle5 | movlw | $\mathrm{h}^{\prime} \mathrm{EA}^{\prime}$ |
|  | movwf | fr_cnt |
|  | movlw | h'FA' |
|  | movwf | fr_cnt2 |
|  | call | dir_chg |
|  | call | ramp_rou |


| set2_cycle6 | movlw movwf movlw movwf call call | $h^{\prime} E C^{\prime}$ <br> fr_cnt <br> h'F9' <br> fr_cnt2 <br> dir_chg <br> ramp_rou |
| :---: | :---: | :---: |
| set2_cycle7 | movlw movwf movlw movwf call call | h'ED' <br> fr_cnt <br> h'F7' <br> fr_cnt2 <br> dir_chg <br> ramp_rou |
| set2_cycle 8 | movlw <br> movwf <br> movlw <br> movwf <br> call <br> call | $h^{\prime} E E^{\prime}$ <br> fr_cnt <br> h'F6' <br> fr_cnt2 <br> dir_chg <br> ramp_rou |
| set2_cycle9 | movlw <br> movwf <br> movlw <br> movwf <br> call <br> call | $h^{\prime} E F^{\prime}$ <br> fr_cnt <br> h'F5' <br> fr_cnt2 <br> dir_chg <br> ramp_rou |
| set2_cycle10 | movlw <br> movwf <br> movlw <br> movwf <br> call <br> call | h'F1' <br> fr_cnt <br> h'F4' <br> fr_cnt2 <br> dir_chg <br> ramp_rou |
| set2_cycle11 | movlw <br> movwf <br> movlw <br> movwf <br> call <br> call | h'F2' <br> fr_cnt <br> h'F2' <br> fr_cnt2 <br> dir_chg <br> ramp_rou |
| delayl | movlw movwf | $\begin{aligned} & \mathrm{h}^{\prime} \mathrm{FF}^{\prime} ; \\ & \text { cnt2 } \end{aligned}$ |


| Con | movlw | h'FF' |
| :--- | :--- | :--- |
|  | movwf | cnt1 |
|  | decfsz | cnt1,1 |
|  | goto | $\$-1$ |
|  | decf | cnt2,1 |
|  | movf | cnt2,w |
|  | subwf | fr_cnt,w |
|  | btfss | status,Z |
|  | goto | Con |
|  | return |  |
|  |  |  |
|  | movlw | h'FF' $^{\prime}$ |
|  | movwf | cnt2 |
|  | movlw | h'FF $^{\prime}$ |
|  | movwf | cnt1 |
|  | decfsz | cnt1,1 |
|  | goto | $\$-1$ |
|  | decf | cnt2,1 |
|  | movf | cnt2, |
|  | subwf | fr_cnt2,w |
|  |  |  |
|  | btfss | status, |
|  | goto | Con5 |
|  | return |  |
|  |  |  |

cw

|  | comf | u_term_hi_acce,f |
| :--- | :--- | :--- |
| comf | u_term_lo_acce,f |  |
| movf | u_term_hi_acce,w |  |
| sublw | b'00000000' $\quad ;$ Upper byte error value (3.1-3)v |  |
| btfsc | STATUS,z |  |
| call | upperbyte |  |




|  | call <br> movwf <br> btfsc <br> call <br> call | upperbyte2 <br> test_bytelo <br> STATUS, c <br> set2_cycle1 <br> clr_drive |
| :---: | :---: | :---: |
| upperbyte | movf <br> sublw <br> movwf <br> btfsc <br> call | u_term_lo_acce,w <br> b'00010100' ;lower byte error value (3.1-3)v <br> test_bytehi <br> STATUS, c <br> set2_cycle11 |
| upperbyte2 | movf <br> sublw <br> movwf <br> btfsc <br> call <br> call | ```u_term_lo_acce,w b'00101001' ;lower byte error value (3.2-3)v test_bytehi STATUS, c set2_cycle11 val_test11``` |
| upperbyte3 | movf <br> sublw <br> movwf <br> btfsc <br> call <br> call | $\begin{aligned} & \text { u_term_lo_acce,w } \\ & \text { b'00111101' }^{\text {test_bytehi }} \text {;lower byte error value (3.3-3)v } \\ & \text { STATUS,c } \\ & \text { set2_cycle10 } \\ & \text { val_test10 } \end{aligned}$ |
| upperbyte4 | movf <br> sublw <br> movwf <br> btfsc <br> call <br> call | u_term_lo_acce,w <br> b'01010010' ;lower byte error value (3.4-3)v <br> test_bytehi <br> STATUS, c <br> set2_cycle9 <br> val_test9 |
| upperbyte5 | movf <br> sublw <br> movwf <br> btfsc <br> call <br> call | u_term_lo_acce,w <br> b'01100110' ;lower byte error value (3.5-3)v <br> test_bytehi <br> STATUS, c <br> set2_cycle8 <br> val_test8 |
| upperbyte6 | movf <br> sublw <br> movwf <br> btfsc | u_term_lo_acce,w <br> b'01111011' ;lower byte error value (3.6-3)v <br> test_bytehi <br> STATUS, c |


|  | call | set2_cycle7 |
| :--- | :--- | :--- |
| call | val_test7 |  |
| upperbyte7 |  |  |
|  | movf | u_term_lo_acce,w |
|  | sublw | b'10001111' $\quad$;lower byte error value (3.7-3)v |
|  | movwf | test_bytehi |
|  | call | STATUS,c |
|  | call | set2_cycle6 |
|  | val_test6 |  |


| upperbyte 12 <br> $3) \mathrm{v}$ | movf | u_term_lo_acce,w ;lower byte error value (4.2- |
| :--- | :--- | :--- |
|  | sublw | b'11110110' $^{\text {movwf }}$ |
| test_bytehi |  |  |
|  | btfsc | STATUS,c |
| call | set2_cycle1 |  |
| call | valtest1 |  |

Overall balancing program (Gyro only) (MPLAB)

$$
\begin{array}{ll}
\text { List } & \mathrm{p}=16 \mathrm{~F} 877 \mathrm{a} \\
& \text { include "p16f877a.inc" } \\
& \text { _config _cp_off \& _wdt_off \& _xt_osc \& _pwrte_on }
\end{array}
$$

| cnt1 | equ | 2 AH |
| :--- | :--- | :--- |
| cnt2 | equ | 2 CH |
| cnt3 | equ | 2 DH |
| cnt4 | equ | 2 EH |
| cnt5 | equ | 3 BH |
| num_times | equ | 3 DH |
| fr_cnt | equ | 3 FH |
| fr_cnt2 | equ | 7 AH |
| fr_cnt1 | equ | 7 BH |
| test_bytehi | equ | 6 AH |
| test_bytelo | equ | 6 CH |
| gy_calc_angle_vel_new_hi | equ | 20 H |
| gy_calc_angle_vel_new_lo | equ | 21 H |
| gy_calc_angle_new_hi | equ | 22 H |
| gy_calc_angle_new_lo | equ | 23 H |
| tilt_temp_hi | equ | 24 H |
| tilt_temp_lo | equ | 25 H |
| Kt_tilt_hi | equ | 26 H |
| Kt_tilt_lo | equ | 27 H |
| Kv_tilt_hi | equ | 28 H |
| K__tilt_lo | equ | 29 H |
| Ka_tilt_hi | equ | 30 H |
| K__tilt_lo | equ | 31 H |
| tilt_rate_hi | equ | 32 H |
| tilt_rate_term_lo | equ | 33 H |
| gy_calc_angle_old_hi | equ | 34 H |
| gy_calc_angle_old_lo | equ | 35 H |
| gy_calc_angle_vel_old_hi | equ | 36 H |
| gy_calc_angle_vel_old_lo | equ | 37 H |
| u_term_hi | equ | 38 H |
| u_term_lo | equ | 39 H |
| Time_lo | equ | 40 H |
| Time_hi | equ | 41 H |
| set_point_lo | equ | 43 H |
| set_point_hi | equ | 45 H |
| prod_res0 | equ | 54 H |
| prod_res1 | equ | 53 H |
|  |  |  |


| prod_res2 | equ | 52 H |
| :--- | :--- | :--- |
| prod_res3 | equ | 51 H |
| Arg_hi | equ | 57 H |
| Arg_lo | equ | 58 H |
| Sum_hi | equ | 59 H |
| Sum_lo | equ | 60 H |
| var_hi | equ | 61 H |
| var_lo | equ | 62 H |
| pwm_bit_cnt | equ | 63 H |
| pwm_bit | equ | 64 H |
| pwm_bit_cnt2 | equ | 65 H |
| pwm_bit2 | equ | 66 H |
| count | equ | 67 H |
| TILT_RATE_LO | equ | 68 H |
| tilt_term_hi | equ | 69 H |
| tilt_term_lo | equ | 70 H |
| tilt_rate_term_hi | equ | 71 H |
| temp_lo | equ | 72 H |
| gy_temp_angle_old_hi | equ | 73 H |
| gy_temp_angle_old_lo | equ | 74 H |
| tiltthi | equ | 75 H |
| tilt_lo | equ | 76 H |
| ramp_cnt | equ | 77 H |
| ramp_cnt2 | equ | 78 H |

```
; Start at the reset vector
org 0x000
goto start
```

Start

| bsf | STATUS,RP0 | ;Bank 1 |
| :---: | :---: | :---: |
| bcf | STATUS,RP1 |  |
| clrf | TRISB | ;PORTB [7-0] outputs |
| movlw | $\mathrm{b}^{\prime} 10000000{ }^{\prime}$ |  |
| movwf | ADCON1 | ;Right justified, all A/D |
| movlw | b'00000000' |  |
| movwf | OPTION_REG |  |
| bcf | STATUS,RP0 | ;Bank 0 |
| movlw | B'01011001' | ;Fosc/8 [7-6], A/D ch3 [5-3], A/D on [0] |
| movwf | ADCON0 |  |
| clrf | PORTB |  |
| clrf | cnt3 |  |
| clrf | num_times |  |
| movlw | d'8' |  |
| movwf | num_samples |  |

```
Main
    call ad_portb
    goto Main
ad_portb
    bsf ADCON0,GO
Wait
    btfsc ADCON0,GO
    goto Wait
;tilt error value = (ADC(x)-3.0)
comp_ute
\begin{tabular}{ll} 
movwf & Arg_lo \\
movf & ADRESH,w ; Store in ADC 10-bit result \\
movwf & Arg_hi ; register \\
movf & temp_acchi,w \\
movwf & Sum_hi \\
movf & temp_acclo,w \\
movwf & Sum_lo \\
& \\
call & add \\
movf & Sum_hi,w \\
movwf & gy_calc_angle_new_hi \\
movf & Sum_lo,w \\
movwf & gy_calc_angle_new_lo \\
decfsz & num_samples \\
call & wait \\
movlw & d'8' \\
movwf & num_samples \\
& \\
movf & gy_calc_angle_new_hi,w \\
movwf & Arg_hi \\
movf & gy_calc_angle_new_lo,w \\
movwf & Arg_lo \\
movlw & b'000000010' \\
movwf & Sum_hi \\
movlw & b'000000001' \\
movwf & Sum_lo \\
call & substract \\
movf & Sum_hi,w \\
movwf & tilt_temp_hi \\
movf & tilt_temp_hi,w \\
&
\end{tabular}
```

| movwf |  | Arg_hi |
| :---: | :---: | :---: |
| movf |  | Sum_lo,w |
| movwf |  | tilt_temp_lo |
| movf |  | tilt_temp_lo,w |
| movwf |  | Arg_lo |
| movlw |  | b'00000000' |
| movwf |  | Kt_tilt_hi |
| movf |  | Kt_tilt_hi,w |
| movwf |  | var_hi |
| movlw |  | $\mathrm{b}^{\prime} 00000001{ }^{\prime}$ |
| movwf |  | Kt_tilt_lo |
| movf |  | Kt_tilt_lo,w |
| movwf |  | var_lo |
| call |  | mul |
| movf |  | prod_res1,w |
| movwf |  | tilt_hi |
| movf |  | prod_res0,w |
| movwf |  | tilt_lo |
| movlw |  | b'00000000' |
| movwf |  | Kv_tilt_hi |
| movlw |  | b'00000001' |
| movwf |  | Kv_tilt_lo |
| movf |  | Kv_tilt_hi,w |
| movwf |  | Arg_hi |
| movf |  | Kv_tilt_lo,w |
| movwf |  | Arg_lo |
| movf |  | tilt_hi,w |
|  | movwf | var_hi |
| movf |  | tilt_lo,w |
|  | movwf | var_lo |
| call |  | mul |
| movf |  | prod_res1,w |
| movwf |  | u_term_hi |
| movf |  | prod_res0,w |
| movwf |  | u_term_lo |
| movf |  | ADRESH,w |
| sublw |  | b'00000010' ; Upper byte for analog value 3V |
| call |  | no_drive |
| movwf |  | temp_lo |
| btfsc |  | STATUS, c |
| call |  | ccw |
| call |  | cw |

The following program is similar to the list of program from pg 94 , no-drive subroutine to pg 109 .

## Multiplication program

Mul

|  | ;movlw |  | 0010' |
| :---: | :---: | :---: | :---: |
|  | ;movwf | Arg |  |
|  | ;movlw |  | $1000{ }^{\prime}$ |
|  | ;movwf | Arg |  |
|  | ;movlw |  | 0100' |
|  | ;movwf | var |  |
|  | ;movlw |  | 0000' |
|  | ;movwf | var |  |
|  | clrf | prod_res0 |  |
|  | clrf | prod_res1 |  |
|  | clrf | prod_res2 |  |
|  | clrf | prod_res3 |  |
|  | clrf | count |  |
|  | movlw | $\mathrm{d}^{\prime} 17{ }^{\prime}$ |  |
|  | movwf | count |  |
| program | movf | var_lo,w | ; Place the value from other ;loop |
| movwf | prod_res0 | ;int <br> ;mu | he variable of this olication loop. |
|  | btfss | status, Z | ;Check whether the product_res0 is zero |
|  | call | Check_n |  |
|  | movf | var_hi,w | ;the product_res0 is zero |
|  | movwf | prod_res1 | ;Check the next upper byte. |
|  | btfsc | status,z |  |
|  |  | equal_zero |  |
| Check_n | btfss | status, c |  |
|  | Call | add_var |  |
|  | movf | var_hi,w |  |
|  | Movwf | prod_res1 |  |
| Check_Arg | movf <br> btfss | Arg_Lo,f status,z | ;Test if value of Arg_Lo is zero |


|  | call <br> movf <br> btfsc <br> call <br> call | test_lsb Arg_Hi,w status,_Z equal_zero | ;Arg_lo is not zero <br> ;Arg_lo is zero <br> ;Test if value of Arg_Hi is zero <br> ;Arg_Hi is equal to zero |
| :---: | :---: | :---: | :---: |
| add_var | incf <br> movf <br> movwf | prod_res1 <br> var_hi,w <br> prod_res1 |  |
| test_lsb | bcf | status, c |  |
|  | rrf | prod_res3 |  |
|  | rrf | prod_res2 |  |
|  | rrf | prod_res1 |  |
|  | rrf | prod_res0 |  |
|  | btfss | status, c | ;Test if there is carry bit |
|  | call | shift | ; There is no carry |
|  | movf addwf | $\begin{aligned} & \text { Arg_lo,w } \\ & \text { prod_res2,f } \end{aligned}$ | ;Upper two bytes is added with the bytes ;of the Arg_Hi:Arg_Lo. |
|  | Btfsc | status, |  |
|  | call | Add_Hi |  |
|  | movf | Arg_Hi,w |  |
|  | addwf | prod_res3,f |  |
|  | call | shift |  |
| equal_zero | clrf | prod_res0 | ; the multiplication result is zero. |
|  | clrf | prod_res1 |  |
|  | clrf | prod_res2 |  |
|  | clrf | prod_res3 |  |
|  | call | stop | ;Exit from the mul subroutine |
| Add_Hi | incf | prod_res3 |  |
|  | Movf | Arg_Hi,w |  |
|  | Addwf | prod_res3 |  |
| shift | decfsz | count |  |
|  | call | test_1sb |  |
|  |  |  |  |
| stop clrf | count |  |  |

## Division program

Division

|  | ;movlw | $\mathrm{b}^{\prime} 00010010^{\prime}$ | ;Inserting the values into divisor and the |
| :---: | :---: | :---: | :---: |
|  | ;movwf | divisor0 | ;number to be divided. |
|  | ;movlw | $\mathrm{b}^{\prime} 00011000{ }^{\prime}$ |  |
|  | ;movwf | divisor1 |  |
|  | ;movlw | $\mathrm{b}^{\prime} 00111000{ }^{\prime}$ |  |
|  | ;movwf | divisor2 |  |
|  | ;movlw | $\mathrm{b}^{\prime} 01001000{ }^{\prime}$ |  |
|  | ;movwf | divisor3 |  |
|  | ;movlw | $\mathrm{b}^{\prime} 10010100^{\prime}$ |  |
|  | ;movwf | prod_res0 |  |
|  | ;movlw | $\mathrm{b}^{\prime} 01110000{ }^{\prime}$ |  |
|  | ;movwf | prod_res1 |  |
|  | ;movlw | $\mathrm{b}^{\prime} 00000100{ }^{\prime}$ |  |
|  | ;movwf | prod_res2 |  |
|  | ;movlw | $\mathrm{b}^{\prime} 11100000{ }^{\prime}$ |  |
|  | ;movwf | prod_res3 |  |
| Clrf | rem_dr0 | ;Initialise va | ables by clearing all the values |
|  | Clrf | rem_dr1 |  |
|  | clrf | rem_dr2 |  |
|  | clrf | rem_dr3 |  |
|  | clrf | Quo_0 |  |
|  | clrf | Quo_1 |  |
|  | clrf | Quo_2 |  |
|  | clrf | Quo_3 |  |
|  | Movlw | 32 |  |
|  | Movwf | bitcnt |  |
| Loop | rlf | prod_res0 | ;Clear the 32 bit result registers |
|  | rlf | prod_res1 |  |
|  | rlf | prod_res2 |  |
|  | rlf | prod_res3 |  |
|  | rlf | rem_dr0 |  |
|  | rlf | rem_dr1 |  |
|  | rlf | rem_dr2 |  |
|  | rlf | rem_dr3 |  |


| movf | divisor3,w <br> subwf <br> btfss <br> call | ;Compare d rem_dr3,w STATUS,z test_more3 | sor and remainder <br> ;test if rem_dr3 is more than divisor if not |
| :---: | :---: | :---: | :---: |
| equal | movf | divisor2,w | ;High byte is equal, so test the lower byte |
|  | btfss | STATUS, z |  |
|  | call | test_more2 |  |
|  | movf | divisor1,w | ;Test the lower bytes |
|  | subwf | rem_dr1,w |  |
|  | btfss | STATUS, z |  |
|  | call | test_more1 |  |
|  | movf | divisor0 |  |
|  | subwf | rem_dr0,w |  |
|  |  | test_more0 |  |

;These sections are to test the result byte whether the divisor value is ;larger or smaller than the rem_dr value.
;If the rem_dr value is larger then the divisor then goto subs subroutine

| test_more3 | btfss <br> call <br> call | STATUS,c <br> last <br> subs2 |
| :---: | :--- | :--- |
| test_more2 | btfss <br> call <br> call | STATUS,c <br> last <br> subs1 |
| test_more1 | btfss <br> call <br> call | STATUS,c <br> last <br> subs0 |
| test_more0 | btfss <br> call <br> bsf <br> call | STATUS,c <br> last <br> prod_res0,0 <br> last |
|  |  |  |

;These sections subs2, subs1 and subs3 are to compare ;the adjacent bytes on whether there is any carry bits. ;If there is any carry, adjust affected bytes by decresing one ;bit value

| subs2 | movf <br> subwf <br> btfss <br> decf <br> movf <br> subwf <br> movf <br> subwf <br> btfss <br> decf <br> movf <br> subwf <br> movf <br> subwf <br> btfss <br> decf <br> movf <br> subwf <br> bsf <br> call | divisor2,w <br> rem_dr2,w <br> STATUS, c <br> rem_dr3 <br> divisor3,w <br> rem_dr3,w <br> divisor1,w <br> rem_dr1,w <br> STATUS, c <br> rem_dr2 <br> divisor2,w <br> rem_dr2,w <br> divisor0,w <br> rem_dr0,w <br> STATUS, c <br> rem_dr1 <br> divisor1,w <br> rem_dr1,w <br> prod_res0,0 <br> last |
| :---: | :---: | :---: |
| subs1 | movf <br> subwf <br> btfss <br> decf <br> movf <br> subwf <br> movf <br> subwf <br> btfss <br> decf <br> movf <br> subwf <br> bsf <br> call | divisor1,w <br> rem_dr1,w <br> STATUS, c <br> rem_dr2 <br> divisor2,w <br> rem_dr2,w <br> divisor0,w <br> rem_dr0,w <br> STATUS, c <br> rem_drl <br> divisor1,w <br> rem_dr1,w <br> prod_res0,0 <br> last |
| subs0 | movf <br> subwf <br> btfss <br> decf <br> movf <br> subwf <br> bsf <br> call | divisor0,w <br> rem_dr0,w <br> STATUS, c <br> rem_dr1 <br> divisor1,w <br> rem_dr1,w <br> prod_res0,0 <br> last |

last | decfsz | bitcnt | ;Test whether 32 rotations has been |
| :--- | :--- | :--- |
| Goto | loop | ;executed |
| Movf | prod_res0,w |  |
| Movwf | Quo_0 | ;Result is stored in Quo variables |
| Movf | prod_res1,w | ;The result is 32 bits values |
|  | Movwf | Quo_1 |
| Movf | prod_res2,w |  |
| Movwf | Quo_2 |  |
| Movf | prod_res3,w |  |
|  | Movwf | Quo_3 |

End

## Programming flow-chart (On h-bridge (bi-direction motor turn))




Direction change subroutine


## Data Acqusition flow chart



## Gyro-Accelerometer

;If one of the portc, 2 exhibit a 1 signal then use the accelerometer data ;If portc, 2 exhibit a 0 signal then use the gyro data ;Both the accelerometer and gyro run simulaneously ;Refer to the CD for more details
$\left.\begin{array}{lll}\text { Data_chg } & \begin{array}{l}\text { btfsc } \\ \text { call } \\ \text { call }\end{array} & \begin{array}{l}\text { PORTC,2 } \\ \text { acce_data } \\ \text { gyro_data }\end{array} \\ \text { acce_data } & \begin{array}{l}\text { movf } \\ \text { movwf } \\ \text { movf } \\ \text { movwf } \\ \text { return }\end{array} & \begin{array}{l}\text { u_term_lo_acce,w } \\ \text { u_term_lo }\end{array} \\ \text { u_term_hi_acce,w } \\ \text { u_term_hi }\end{array}\right]$

